Overview

- Bioconductor Project
- Fold changes
- Tiling Arrays for ChIP-chip
- Tiling Arrays for Transcript Profiling

Wolfgang Huber EMBL/EBI



- Biology is becoming a computational science
- Problems of data analysis and mathematical modeling require computational support and computational solutions
- We put a premium on code reuse
 - many of the tasks have already been solved
 - if we use those solutions we can put effort into new research
- Data complexity is dealt with using well designed, self-describing data structures
- Reproducible research requires open access to computational code

The S language

- The S language has been developed since the late 1970s by John Chambers and his colleagues at Bell Labs.
- The language has been through a number of major changes but has been relatively stable since the mid 1990s
- The language combines ideas from a variety of sources (e.g. *Awk*, *Lisp*, *APL*...) and provides an environment for quantitative computations and visualization.

Implementations

- S-Plus a commercialization of the Bell Labs code.
- R an independent open source version that was originally developed at the University of Auckland but which is now
- developed by a world wide group of developers.
- Each version has advantages and problems.

References

- The New S Language, Statistical models in S, Programming with Data, by John Chambers and various co-authors
- Modern Applied Statistics, S Programming by W. N. Venables and B. D. Ripley
- Introductory Statistics with R by P. Dalgaard
- *Data Analysis and Graphics Using R* by J. Maindonald and J. Braun.

Packages

- Packages are the main unit of software authoring, versioning and distribution
- CRAN is the major repository for R packages. It is hosted by TU Vienna and ETH Zürich, and has many mirrors worldwide
- Bioconductor is a repository for biology related packages. It is hosted at the Fred Hutchinson Cancer Research Centre.



- an open source and open development software project for the analysis of biomedical and genomic data.
- was started in the autumn of 2001 and includes core developers in the US, Europe, and Australia.
- R and the R package system are used to design and distribute software.
- A goal of the project is to develop software modules that are integrated and which make use of available web services to provide comprehensive software solutions to relevant problems.

Goals of the Bioconductor project

- Provide access to powerful statistical and graphical methods for the analysis of genomic data.
- Facilitate the integration of biological metadata (e.g. Entrez, Ensembl, GO(A), PubMed) in the analysis of experimental data.
- Allow the rapid development of extensible, interoperable, and scalable software.
- Promote high-quality documentation and reproducible research.
- Provide training in computational and statistical methods.

Why are we Open Source

- so that you can find out what algorithm is being used, and how it is being used
- so that you can modify these algorithms to try out new ideas or to accommodate local conditions or needs
- so that they can be used as components (potentially modified)

Component software

- most interesting problems will require the coordinated application of many different techniques
- thus we need integrated interoperable software
- web services are one tool
- well designed software modules are another
- you should design your piece to be a cog in a big machine

Data complexity

Dimensionality.

- Dynamic/evolving data: e.g., gene annotation, sequence, literature.
- Multiple data sources and locations: inhouse, WWW.
- Multiple data types: numeric, textual, graphical.

No longer X_{nxp}!

We distinguish between biological metadata and experimental metadata.

Bioconductor packages Release 1.9, Oct 2006 ~200 Packages

General infrastructure

Biobase, BioStrings, graph, multtest

Annotation:

annotate, biomaRt, annaffy, AnnBuilder -- data packages.

Graphics:

geneplotter, hexbin

Pre-processing Affymetrix oligonucleotide chip data:

affy, gcrma, affycomp

Pre-processing other array types

limma, beadarray vsn, marray, arrayMagic

Differential gene expression:

limma, genefilter, GOstats, siggenes, Category Graphs and networks:

graph, RBGL, Rgraphviz, GOstats. Other data: prada, EBImage, DNAcopy, aCGH

Affymetrix preprocessing

- Traditional Affymetrix genechips: calculation of per-transcript expression level estimates from the hybridization intensities
- Background correction, Between-chip normalization, Probe set summarization
- Manufacturer's original algorithm was highly unprecise + problematic
- Many academics started to develop their alternatives, leading to vast improvement in the data quality of the technology
- This was one of the first "success stories" of Bioconductor

Affycomp: a benchmark for Affymetrix genechip expression measures

o Data: Spike-in (Affymetrix)

16 genes, 14 concentrations, complex background Dilution series (GeneLogic) 60 × HGU95Av2, liver & CNS cRNA in different proportions and amounts

o Benchmark:

15 quality measures regarding

- -reproducibility
- -sensitivity
- -specificity

Put together by Rafael Irizarry (Johns Hopkins) http://affycomp.biostat.jhsph.edu

Precision vs accuracy

←bias

accuracy→

variance→

precision











Figure 5a): A typical identification rule for differential expression filters genes with fold change exceeding a given threshold. This figure shows average ROC curves which offer a graphical representation of both specificity and sensitivity for such a detection rule. Average ROC curves based on comparisons with nominal fold changes ranging from 2 to 4096. b) As a) but with nominal fold changes equal to 2.





BioC2007, Fred Hutchison Research Center

August 2007

Developer's meeting and package demonstrations



Book

Statistics for Biology and Health

Robert Gentleman Wolfgang Huber Sandrine Dudoit Editors

Bioinformatics and Computational Biology Solutions Using R and Bioconductor Preprocessing and normalization of microarray data, cell-based assays, mass spectrometry

Uni- and multivariate statistical analysis methods

Machine Learning

Harvesting and using metadata from biological databases

Visualization

Graphs and Networks in molecular biology

Including the software code (R) to reproduce all examples, figures etc.



Bioconductor

- Bioconductor core team
- Ben Bolstad, **UC Berkeley**
- Vince Carey, Channing Laboratory, Harvard
- Sandrine Dudoit, Biostatistics, UC Berkeley
- Seth Falcon, FHCRC
- Robert Gentleman, FHCRC
- Wolfgang Huber, EMBL/EBI
- Rafael Irizarry, Biostatistics, Johns Hopkins
- Nianhua Li, FHCRC
- Li Long, ISB, Lausanne
- Jim MacDonald, **U Michigan**
- Martin Morgan, FHCRC
- Herve Pages, FHCRC
- Gordon Smyth, WEHI
- Yee Hwa (Jean) Yang, Sydney

ratios and fold changes

Fold changes are useful to describe continuous changes in expression



But what if the gene is "off" (below detection limit) in one condition?



- Many interesting genes will be off in some of the conditions of interest
- Due to unspecific hybridization and optical noise, measured values are always > 0.
- 1. If you want expression measure to be an unbiased estimator of abundance
- \Rightarrow strong background correction, get many values \leq 0
- \Rightarrow need something else than (log)ratio
- 2. If you let expression measure be biased (always>0)
- \Rightarrow weak background correction, then can keep ratios.
- \Rightarrow how do you choose the bias?

Sources of variation

amount of RNA in the sample efficiencies of

- -RNA extraction
- -reverse transcription
- -labeling
- -fluorescent detection

Systematic

similar effect on many measurements
corrections can be estimated from data

Calibration

probe purity and length distribution cross-/unspecific hybridization stray signal

Stochastic

o too random to be explicitely accounted for o remain as "noise"

Error model



measured intensity = offset + gain × true abundance $Y_{ik} = a_{ik} + b_{ik} X_{k}$ $a_{ik} = a_i + \varepsilon_{ik}$

 a_i per-sample offset $\varepsilon_{ik} \sim N(0, b_i^2 s_1^2)$ "additive noise"

$$b_{ik} = b_i b_k \exp(\eta_{ik})$$

- b_i per-sample normalization factor
- b_k sequence-wise probe efficiency

 $\eta_{ik} \sim N(0, s_2^2)$ "multiplicative noise"

The two-component model



B. Durbin, D. Rocke, JCB 2001

variance stabilizing transformations

X_{μ} a family of random variables with $EX_{u}=u$, $VarX_{u}=v(u)$. Define $f(x) = \int \frac{1}{\sqrt{v(u)}} du$ \Rightarrow var $f(X_u) \approx$ independent of u

derivation: linear approximation

variance stabilizing transformations



variance stabilizing transformations

$$f(x) = \int_{-\infty}^{x} \frac{1}{\sqrt{v(u)}} du$$

- 1.) constant variance ('additive') $v(u) = s^2 \implies f \propto u$
- 2.) constant CV ('multiplicative') $v(u) \propto u^2 \Rightarrow f \propto \log u$
- 3.) offset $v(u) \propto (u + u_0)^2 \Rightarrow f \propto \log(u + u_0)$

4.) additive and multiplicative

$$v(u) \propto (u + u_0)^2 + s^2 \Rightarrow f \propto \operatorname{arsinh} \frac{u + u_0}{s}$$

the "glog" transformation



variance stabilization





parameter estimation

 $\frac{-a_{i}}{2} = \mu_{k} + \varepsilon_{ki},$ $\operatorname{arsinh}^{\mathbf{y}_{ki}}$ $\varepsilon_{ki} \sim N(0, c^2)$ maximum lik gain * true abundance measured intensity = offset + - but sensitiv $\boldsymbol{y}_{ik} = \boldsymbol{a}_{ik} + \boldsymbol{b}_{ik} \boldsymbol{x}_{ik}$ o model holds differentially $b_{ik} = b_i b_k \exp(\eta_{ik})$ $a_{ik} = a_i + \mathcal{L}_{ik} + \mathcal{E}_{ik}$ o robust varid b_i per-sample a_i per-sample offset normalization factor Trimmed Sum L_{ik} local background b_k sequence-wise provided by image labeling efficiency analysis o works well $\eta_{ik} \sim N(0, s_2^2)$ $\varepsilon_{ik} \sim N(0, b_i^2 s_1^2)$ differentially "multiplicative noise" "additive noise"

Least trimmed sum of squares regression



- least trimmed sum of squares

glog



- For Affymetrix data, it turns out that the weak background correction method of RMA and the glog(-ratio) of vsn result in very similar results
- vsn also useful for other array platforms (e.g. spotted two-color)
- Don't be afraid of the "glog", it is equivalent to weak (=biased) background correction and normal log!
- vsn package (see vignette)
- Ref.: Huber, von Heydebreck et al., Bioinformatics 2002

Reproducible Research and Compendia

There is a tendency to accept seemingly realistic computational results, as presented by figures and tables, without any proof of correctness.

F. Leisch, T. Rossini, Chance 16 (2003)

We re-analyzed the breast cancer data from van't Veer et al. (2002). ... Even with some help of the authors, we were unable to exactly reproduce this analysis.

R. Tibshirani, B. Efron, SAGMB (2002)

Re-analysis of a breast cancer outcome study

- E. Huang et al., Gene expression predictors of breast cancer outcome, The Lancet 361 (9369): 1590-6 (2003)
- 89 primary breast tumors on Affymetrix Chips (HG-U95av2), among them: 52 with 1-3 positive lymph nodes, 18 led to recurrence within 3 years, 34 did not.
- **Goal: predict recurrence**
- Claim: 5 misclassification errors, 1 unclear (leave-one-out cross-validation)
- Method: Bayesian binary prediction trees (at the time, unpublished)
- http://www.cagp.duke.edu
...we tried to reproduce these results, starting from the published µarray raw data (CEL files) But couldn't.

The paper (and supplements) didn't contain the necessary details to re-implement their algorithm.

Authors didn't provide comparisons to simple well-known methods.

In our hands, all other methods resulted in worse misclassification results.

Is their new Bayesian tree method miles better than everything else?

Or was their analysis over-optimistic? (over-fitting, selection bias)

A general pattern

New publications often present a new microarray data set, and a new classification method.

Merits of the methods, and merits of the data are entangled.

Is it necessary to develop an ideosyncratic method?

Which result could be achieved with standard approaches? (accuracy vs. interpretability)

Is there a big difference and what are the reasons for it ? (errors happen ... in implementation /validation)

Compendia

Interactive documents that contain:

- Primary data
- Processing methods (computer code)
- Derived data, figures, tables and other output
- Text: research report (result, materials and methods, conclusions)

Package compHuang: reanalysis of Huang et al. data, using different classification and preprocessing methods and a correct cross-validation procedure for estimating the prediction error

Based on R/Bioconductor's package and vignette technologies

M. Ruschhaupt, W. Huber, A. Poustka, U. Mansmann, Statistical Applications in Genetics and Molecular Biology (2004)

PLoS Medicine Feb 2005.

source markup (here: latex & R) Sweave

processed document (here: PDF)

<<MCRestimate call,eval=FALSE,echo=TRUE>>= r.forest <- MCRestimate(eset, class.label,</pre> class.function="RF.wrap", select.fun=red.fct,cross.outer=10, cross.inner=5, cross.repeat=20) @ <<rf.save,echo=FALSE,results=hide>>= savepdf(plot(r.forest, main="Random Forest"),"image-RF.pdf") <<result>>= r.forest The final document includes results of the calculation, graphical outputs, tables, and optionally parts of the R-Code which has been used. Also the description of the experiment, the interpretation of the results, and the conclusion can be integrated. In this example we applied our compendium to T. Golubs ALL/AML data~\cite{Golub.1999}. \begin{figure}[h] \begin{center} \includegraphics [width=0.4\textwidth] {image-RF} \end{center} \end{figure} \smallskip <<summary,echo=FALSE>>= method.list <- list(r.forest,r.pam,r.logReg,r.svm)</pre> name.list <- c("RF", "PAM", "PLR", "SVM")</pre> conf.table <- MCRconfusion(method.list, col.names=name.list) <<writinglatex1,echo=FALSE, results=tex>>= xtable(conf.table,"Overall number of misclassifications", label="conf.table",display=rep("d",6)) %\input{samples.1} %\input{conf.table} \begin{thebibliography}{1} \bibitem[Golub et al., 1999] {Golub.1999} Golub TR, Slonim DK, Tamayo P, Huard C, Gaasenbeek M, Mesirov JP, Coller H, Loh ML, Downing JR, Caligiuri MA, Bloomfield CD, Lander ES. \newblock Molecular classification of cancer: class discovery and class prediction by gene expression monitoring \newblock\textit{Science} 286(5439): 531-7 (199 \end{thebibliography}

RF PAM PLR SVM Group size ALL 470 0 0 AML $\mathbf{2}$ 251 All 1 $\mathbf{2}$ 72

Table 1: Overall number of misclassifications

> r.forest <- MCRestimate(eset, class.label, class.function = "RF.wrap", select.fun = red.fct, cross.outer = 10, cross.inner = 5, cross.repeat = 20)

> r.forest

Result of MCRestimate with 20 repetitions of 10-fold cross-validation

Selection function : g.red.highest.var.2000 Cluster function : identity Classification function: RF.wrap

The confusion table: ALL AML class error ALL 47 0 0.00 AML 1 24 0.04

The final document includes results of the calculation, graphical outputs, tables, and optionally parts of the R-Code which has been used. Also the description of the experiment, the interpretation of the results, and the conclusion can be integrated. In this example we applied our compendium to T. Golubs ALL/AML data [Golub et al., 1999].



References

[Golub et al., 1999] Golub TR, Slonim DK, Tamayo P, Huard C, Gaasenbeek M, Mesirov JP, Coller H. Loh ML, Downing JR, Caligiuri MA, Bloomfield CD, Lander ES. Molecular classification of cancer: class discovery and class prediction by gene expression monitoring Science 286(5439): 531-7 (1999).





See also the work by

Donald Knuth HP Wolf Günther Sawitzki Friedrich Leisch Robert Gentleman Duncan Temple Lang



EBI Oleg Sklyar Ligia Bras Elin Axelsson Richard Bourgon Jörn Tödling Paul McGettigan Tineke Casneuf Matt Ritchie

DKFZ

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EMBL Lars Steinmetz Fabiana Perocchi Eugenio Mancera Zhenyu Xu

Florian Hahne Dorit Arlt Stefan Wiemann Annemarie Poustka

Bioconductor Robert Gentleman Seth Falcon Rafael Irizarry Vince Carey

Amy Kiger

evaluation: sensitivity / specificity in detecting differential abundance

o Data: paired tumor/normal tissue from 19 kidney cancers, in color flip duplicates on 38 cDNA slides à 4000 genes.

o 6 different strategies for normalization and quantification of differential abundance

Calculate for each gene & each method: t statistics, permutation-p

o For threshold α , compare the number of genes the different methods find, $\#\{p_i \mid p_i \le \alpha\}$

evaluation: comparison of methods



more accurate quantification of differential expression \Rightarrow higher sensitivity / specificity

Transcript mapping and genotyping with high-resolution tiling arrays

Wolfgang Huber EMBL - EBI

Genechip S. cerevisiae Tiling Array



4 bp tiling path over complete genome (12 M basepairs, 16 chromosomes)
Sense and Antisense strands
6.5 Mio oligonucleotides
5 μm feature size

manufactured by Affymetrix designed by Lars Steinmetz (EMBL & Stanford Genome Center)

RNA Hybridization



Before probe-specific normalization



AT content and (weak) probe response



Probe response

Control vs. control

IgG control (chr 4)



© Richard Bourgon



$$q_i = \log_2 \frac{y_i}{s_i} \circ$$

$$q_i = g \log_2 \frac{y_i - b(s_i)}{s_i} \circ$$

remove 'dead' probes

$$q_i = \text{glog}_2 \frac{PM_i - MM_i}{S_i}$$



Probe-specific response normalization

$$q_i = g \log_2 \frac{y_i - b(s_i)}{s_i}$$

s_i probe specific response factor.

Estimate directly from DNA hybridization data

 $b_i = b(s_i)$ probe specific background term. Estimate from signal of intergenic probes, interpolating to others by assuming that probes with similar s_i have similar b

Estimation of background *b* from intergenic PM probes



After normalization



Segmentation

Two obvious options:

Smoothing and thresholding: simple, but estimates of transcript boundaries will be *biased* and depend on expression level

Hidden Markov Model (HMM): but our "states" come from a continuum, unclear how to discretize

Our solution:





Position

Structural change model (SCM): piecewise constant functions

$$\forall \mathbf{X} \in \left| t_{k-1}, t_{k} \right|$$
:

$$Y(x) = \mu_k + \varepsilon(x)$$

*t*₁,..., *t*_S: change points
Y: normalized intensities
x: genomic coordinates

 μ_k : level of k-th segment

Model fitting



*t*₁,..., *t*_S: change points *J*: number of replicate arrays

Optimization

Naïve optimization has complexity n^s , where $n \approx 10^5$ and $s \approx 10^{3.5}$

Fortunately, there is a dynamic programming algorithm with complexity $O(n^{2)}$, and good heuristic O(n):

$$k = 0, \quad \forall 0 \le i < j \le n \quad \hat{J}_1(i,j) = \sum_{x=i+1}^{j} \left\{ \log(2\pi \times \hat{\sigma}_1^2) + \left[\frac{y(x) - \hat{\mu}_1}{\hat{\sigma}_1}\right]^2 \right\}$$
$$\forall k \in [1, K_{max}] \quad \hat{J}_{k+1}(1,j) = \min_h \left\{ \hat{J}_k(1,h) + \hat{J}_1(h+1,j) \right\}$$

F. Picard, S.Robin, M. Lavielle, C. Vaisse, G. Celeux, JJ Daudin, BMC Bioinformatics (2005)

Bai+Perron, Journal of Applied Econometrics (2003)

Software: W. Huber, package tilingArray, www.bioconductor.org

A. Zeileis, package strucchange, CRAN

Model selection criteria

model family has just one parameter: no. of segments



Confidence Intervals

$$\frac{\left(\Delta_{i}^{t} Q_{i} \Delta_{i}\right)^{2}}{\left(\Delta_{i}^{t} \Omega_{i} \Delta_{i}\right)^{2}} \left(\hat{t}_{i} - t_{i}\right) \Rightarrow \operatorname*{argmax}_{s} V_{i}(s)$$

- Δ_i level difference
- Q_i no. data points per unit *t*
- Ω_i error variance (allowing serial correlations)
- t_i, \hat{t}_i true and estimated change points
- *V_i(s)* appropriately scaled and shifted Wiener process (Brownian motion)

Bai and Perron, J. Appl. Econometrics 18 (2003)

Transcript Mapping by Segmentation

Along-chromosome plots for each strand (available in database): www.ebi.ac.uk/huber-srv/queryGene



A closer look



Mapping of UTRs



UTR lengths for 2044 ORFs



On average

3' UTRs are longer than 5' UTRs

No correlation between 3' and 5' lengths



Transcriptional architectures

921 ORFs were divided into at least two segments



Symbols: * = identical : = strong similarity . = weak similarity

Scer_MET7/YOR241W	1	MHKGKE	(NY	PNI	LΙΤ	SF	RMN	LKK	II	LNH	DRF	SH	ΡEF	RMK	ΤN	ALI	RF	ΤF	VYII	ΚF	50
Sbay_c154_23525																					
Smik c485 21053																					
U Sbay Contig635.23																					
U Scas Contig640.5																					
U Sklu Contig2361.2	1																			- M	1
ols																					

L 4	46
L 4	46
L 4	46
I 4	46
I	51
:	
_	
<mark>.</mark> P	150
Þ	150 96
b b b	150 96 96

RRIGYSTKDYN

KLNIIHITGTKGKGSTAAFTQSILS

P 96

s 101

Operon-like structures

123 segments contained ORFs of more than one protein-coding gene



YCK2

casein kinase I, involved in cytokinesis

GIM3

tubulin binding, involved in microtubule biogenesis



Transcription 6 over active 4 promoters 2

Martens, J. A., Laprade, L. & Winston, F. Intergenic transcription is required to repress the *Saccharomyces cerevisiae* SER3 gene. *Nature* **429**, 571-574 (2004).



Looking for New Transcripts



Isolated

Antisense





CBF1: important for growth in rich media

GO of Genes with antisense: Cell wall, transcriptional regulation, meiotic cell cycle...
Novel transcripts

Sequence conservation (with other yeast species) not more than for other intergenic sequence

No codon signature (3-periodicity of mutation frequencies)

But: conservation of predicted RNA secondary structures



with Lee Bofkin, Nick Goldman

Stephan Steigele, Kay Nieselt Peter Stadler

Cell Cycle



Temperature sensitive cdc28 – arrest at G1 Monitored at 10 min intervals for 230 min in total (~3 cell cycles)





Time (min)



RNA mediated regulation

- UTR lengths associated with function, localization, regulation
- Antisense found predominantly to 3' UTRs and longer UTRs
- Antisense correlated with GO categories
- Similar to patterns for miRNAs in other species

Suggests a functional role for antisense in S. cerevisiae

A Clinical Isolate of S. cerevisiae: YJM789

- Isolated from lung of an AIDS patient
- Pathogenic in mouse model
- Forms pseudohyphae; undergoes colony-morphology switching
- Able to grow at 42°C

YJM789





Laboratory strain



Two Genomes on One Array: Quantifying Allelic Transcription



Local vs distant QTL ...trans vs. cis regulation



PHO84 Allele-specific Expression



BRE4 Allele-specific Expression



Genotyping with Microarrays



Segregation of 50,000 Markers in a Tetrad



YJM789S288c

Genome-wide Map of Recombination Chr I



Position (bp)

Conclusion

- Transcriptional complexity goes far beyond current annotation
- Hundreds of antisense transcripts found
- Allelic variation in transcription detected
- Map of recombination breakpoints



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Robert Gentleman Vince Carey Rafael Irizarry Ben Bolstad Paul Murrell Achim Zeileis Analysis of ChIP-chip experiments

NGFN Course 2006 Wolfgang Huber EMBL/EBI

Chromatin immunoprecipation and DNA-chip



MJ Buck and JD Lieb, Genomics 83 (2004)

Chromatin immunoprecipitation (ChIP)



TF/DNA crosslinking *in vivo*



Sonication



TF-specific antibody



Immunoprecipitation



Crosslink reversal and DNA purification



Amplification



Brief history

Yeast:

DNA-binding sites of individual TFs (Ste12, Gal4, Swi4, Swi6, Rap1): 2000, 2001 "Regulatory network" of 106 TFs: Lee et al. 2002 Condition dependence: Harbison et al. 2004

Mammals: Early experiments 2002, 2003 Limitations: size of genome / no. probes on array; repeated sequence

See Hanlon/Lieb review for more

Protein-DNA interactions

not just transcription factors...

DNA replication Recombination DNA repair

Technological options

Enrichment of the protein of interest:

Specific antibody Tag protein and use tag-specific antibody Tag protein and use tandem affinity purification

Array probes

Spotted PCR product Spotted oligonucleotides In-situ synthesized oligonucleotides (Affymetrix, Nimblegen)

Low-resolution arrays

Low spatial resolution (e.g. 1 data point per 5' upstream region)

Confounding between binding affinity / occupancy and distance from probe to binding site



Controls

Sample: ChIP of interest

There are (at least) two types of control:

Control for array & hybridization variability (esp. in two-color technique), for probe effects (esp. in short oligo technique): genomic DNA ("Input")

Biological control, for sample handling, differential PCR, antibody unspecificity ideal: cells lacking AB epitope but otherwise identical 2nd best: mock IP (no AB)

How should the controls be used?

Hybridization controls: see later - probe response normalization

Biological controls:

- 1. Log-ratio: call enrichment if *log(IP) log(control)* is large
- 2. Conditional: call enrichment if *log(IP)* is large and *log(control)* is small

Biologists seem to prefer 2.

Complications I: Variable formation of DNA-protein crosslinks



(i) Unmodified protein(ii) Modified protein(iii) Another interacting protein is in the way(iv) modified lysine

From Hanlon and Lieb 2004

Formaldehyde:

crosslink proteins by linking amino-group of lysines with adjacent peptide bonds

also DNA-protein (if DNA is partially denatured)

what happens exactly when chromatin is crosslinked in vivo with formaldehyde is not well known.

Complications II: Variable epitope accessibility



(i) epitope detected by ChIP(ii) direct competition(iii) blockage

From Hanlon and Lieb 2004

A physical model for ChIPchip data

Slides from Richard Bourgon + Terry Speed Department of Statistics, UCB

A physical/statistical model for the assay

Step

Model

Source material *N* strands of extracted DNA.

Sonication	Uniform fragmentation of chromatin, with no interference. Probability of a break at any base is θ .
IP	Fragments with no binding site pass with probability ϕ ; fragments with a binding site pass with probability ϕ' , and $\phi' \gg \phi$.
Amplification	Z, a random multiplier for each fragment passing IP. (For PCR, Z is a branching process with <i>t</i> cycles and efficiency <i>p</i> .)

© Richard Bourgon, Department of Statistics, UCB

N source DNA strands


Sonication



Immunoprecipitation



Fragments passing IP



Implications

- This model has implications for...
- -Target abundance: the shape and size of signal near a binding site.
- -Spatial correlation: correlation between nearby observations, both near binding sites and also, significantly, in "background" regions far from binding sites.

Sonication: uniform fragmentation?

Schwarz, Kahn, and Pirrotta (2005), *Mol. Cell Biol.* 25:432-39.

suggest that the *bxd* PRE and *hsp*26 promoter regions lie in lower density chromatin than the *white* coding region, and as a consequence are more sensitive to sonication.

(Marker fragment sizes are in kb.)



PCR: *i.i.d.* amplification multipliers?

Liu, Schreiber, and Bernstein (2003), *BMC Genomics* 4:19-39.

Biases with respect to sequence and fragment length exist, and will be amplified exponentially.



Target abundance

Dependence of expected signal on distance from binding site to probe site



Suppose probe *i* is Δ bases from a binding site τ . Probability that fragment is available for binding to probe:

$$\mathbb{P}(i \sim \tau) \mathbb{P}(X_{in} = 1 | i \sim \tau) + \mathbb{P}(i \not\sim \tau) \mathbb{P}(X_{in} = 1 | i \not\sim \tau)$$
$$= (1 - \theta)^{\Delta} \phi' + (1 - (1 - \theta)^{\Delta}) \phi$$

© Richard Bourgon, Department of Statistics, UCB Note exponential decay from ϕ' to ϕ .

Expected log-ratio



CG69554-RA and RB



Chromosome 2L

Log ratios (unsmoothed) from 3 vs. 3 comparisons, two different IP/PCR/hybridization groups.

CG6604



Summary: shape of expected signal

- Binding sites produce high expected signal in multiple, consecutive probes.
- Shape permits localization of the binding site! In the absence of noise, the binding site coincides with the peak.
- Methods which take shape into account may be more powerful than those that do not.
- -Windowed enrichment estimates will be downwardly biased.
- Calibration/test data with a different signal shape will not accurately represent behavior of true signal.

Spatial correlation in log-ratio



Set 2

For both data sets, there is statistically significant autocorrelation up to a lag of \approx 15 positions.

spacing.

Compute auto-

correlation at

various lags.



Spatial correlation in log-ratio

in unbound regions

$$\operatorname{cor}(LR_i, LR_j) \propto (1-\theta)^{|i-j|}$$

θ related to fragment length distribution

Summary: spatial correlation

Under the model, both target abundance and the intensity log-ratio exhibit positive spatial correlation.

Correlation arises from the relationship between fragment size and probe spacing.

Here we have used the log-ratio statistic to confirm spatial correlation. Correlation in abundance, however, will impact *any* statistical procedure.

Ignoring spatial correlation can produce false positives, producing spurious hits *in both directions*.

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