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# Affy Chips: Cel-file versus summary information

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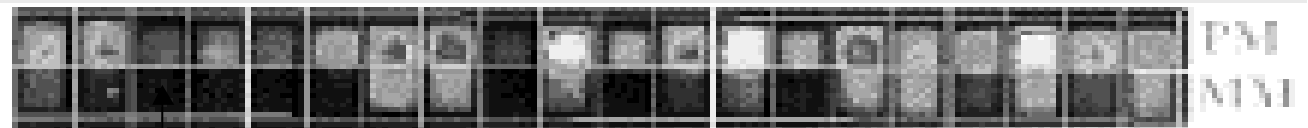
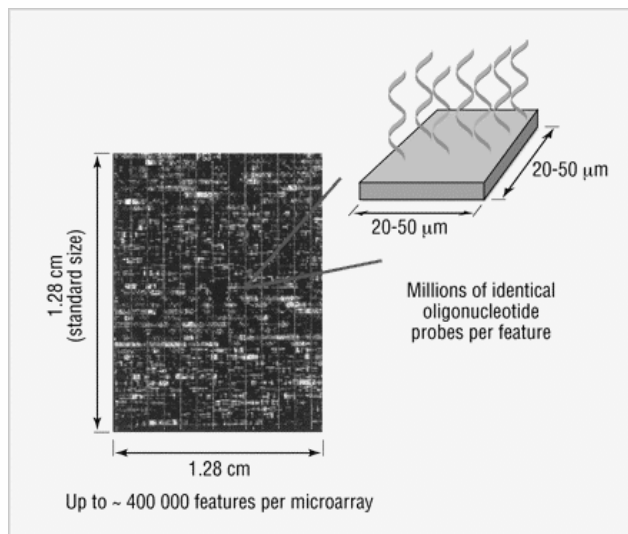
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# Affymetrix technology

5' 3'

16-20 *probe*  
*pairs* per gene

PM: ATGAGCTGTACCAATGCCAACCTGG  
MM: ATGAGCTGTACCTATGCCAACCTGG



64 pixels; Signal intensity is upper quartile of the 36 inner pixels

Stored in CEL file

16-20 probe pairs: HG-U95a  
11 probe pairs: HG-U133

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## Low – level -Analysis

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- Preprocessing signals: background correction, normalization, PM-adjustment, summarization.
- Witt E, McClure J (2004) Statistics for Microarray: design, analysis, and inference, Chichester, John Wiley & Sons
- Noise and Bias
- Differences in sample preparation, variation during mRNA extraction and isolation
- Manufacturing of the array: variation in hybridization efficiency, abundance
- Normalization on probe or probe set level?
- Which probes / probe sets used for normalization
- How to treat PM and MM levels?
- Linear or non-linear normalization?

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## Expression measures based on $d = \text{PM-MM}$

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- AvDiff

$$\text{AvDiff} = \frac{1}{\#A} \sum_{j \in A} (\text{PM}_j - \text{MM}_j) \quad \begin{array}{l} \text{A contains only probes with } d \\ \text{not an outlier} \end{array}$$

- Li & Wong (dChip)

$$\text{Pm}_{ij} - \text{Mm}_{ij} = \theta_i \phi_j + \varepsilon_{ij} \quad \varepsilon_{ij} \sim N(0, \sigma^2)$$

MLE for  $\theta_i$  gives expression measure

- MAS5

$$\begin{aligned} \text{signal} &= \text{Tuckey Biweight}[\text{PM}_j - \text{CT}_j] \\ \text{CT}_j &= \min(\text{MM}_j, \text{PM}_j) \end{aligned}$$

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## Normalization – Baseline Array

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- **Scaling:**

First array is baseline:  $m_{\text{base}}$  mean intensity of baseline array,  $m_i$  ( $i=1, \dots, n$ ) mean intensity of array  $i$ , scale factor for array  $i$ :  $\beta_i = m_{\text{base}} / m_i$ .

Normalized intensity an array  $i$ :  $x_{i,\text{norm}} = x_i \cdot \beta_i$ .

Two options: apply normalisation to probes or after summarization to probe set measures.

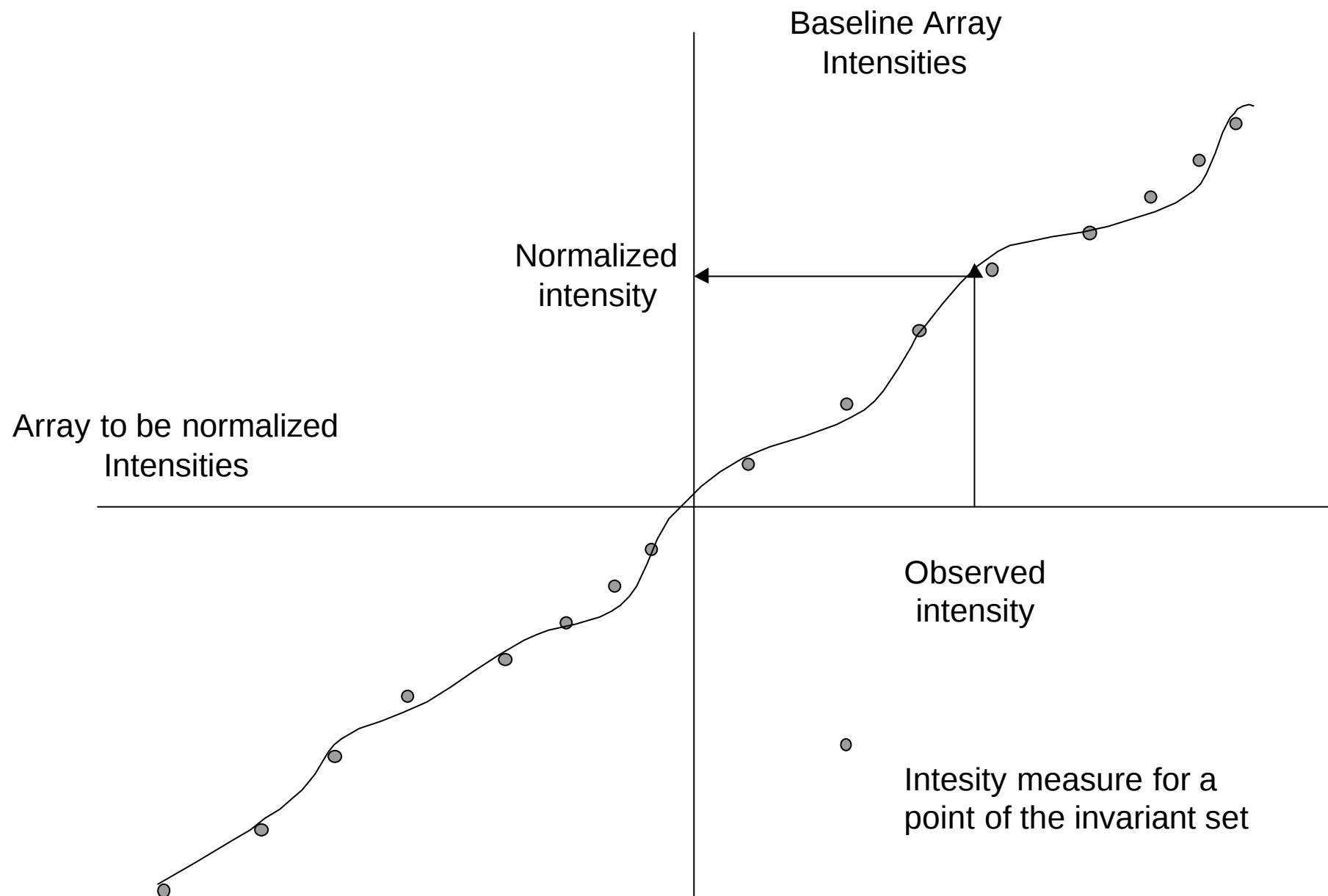
- **Invariant set:**

PM probe values are used only.

Probes which are not differentially expressed (unknown). It is assumed that PM probe signals which not differentially expressed in two arrays have similar intensity ranks ( $r$ ).

Point's proportion rank difference (PRD):  $|(r_{k,i} - r_{k,\text{base}})| / (\# \text{probes})$

Small  $\text{PRD}_{k,i}$  ( $< 0.003, 0.007$ ), include probe into invariant set, cycle through all arrays, use invariant set to create array specific calibration curve by running median.



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## Normalization – complete data methods

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- Quantile normalization:  
Make the distribution of probe intensities the same for all arrays.  
$$F_{i,\text{normalised}}(x) = F_{\text{global}}(F_i^{-1}(x))$$
- Robust quantile normalization
- Cyclic loess (MA plots of two arrays for low-transformed signals and loess)
- Contrast
- RMA
- VSN

What is the best approach? Look at criteria provided by the affycomp procedure.

*Cope LM, Irizarry RM, Jaffee H, Wu Z, Speed TP, **A Benchmark for Affymetrix GeneChip Expression Measures**, Bioinformatics, 2004, 20:323-31*

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## How to approach the quantification of gene expression: Three data sets to learn from

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- **Mouse Data Set (A)**  
5 MG-U74A GeneChip® arrays, 20% of the probe pairs were incorrectly sequenced, measurements read for these probes are entirely due to non-specific binding
- **Spike-In Data Set (B)**  
11 control cRNAs were spiked-in at different concentrations
- **Dilution Data Set (C)**  
Human liver tissues were hybridised to HG-U95A in a range of proportions and dilutions.

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## Feature of probe level data

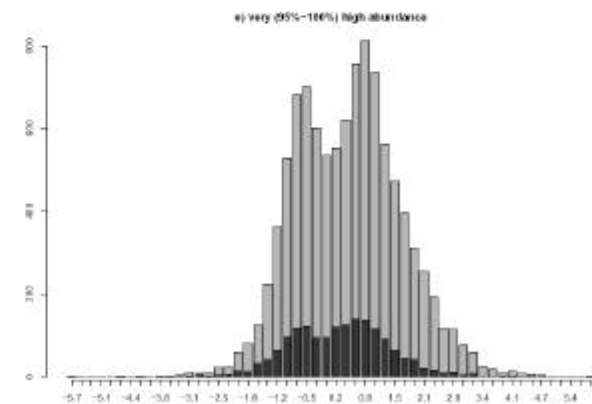
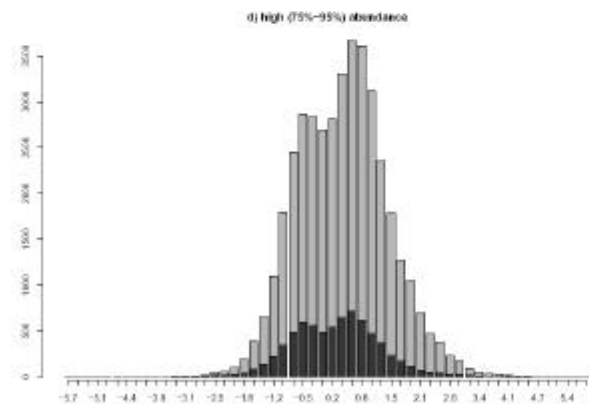
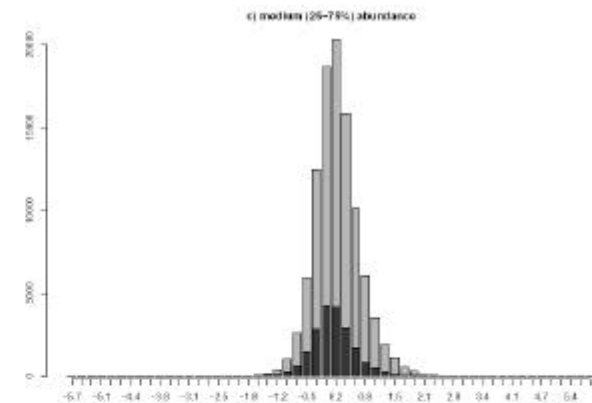
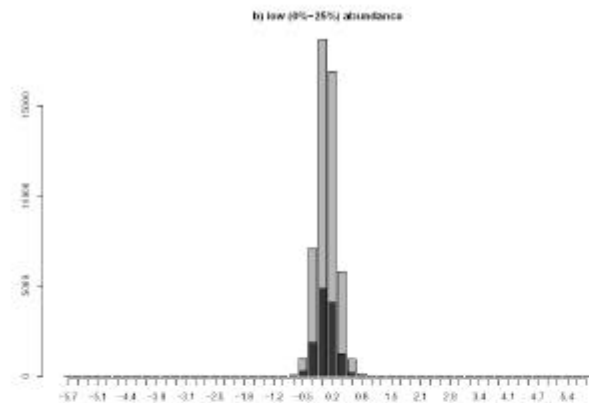
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- MM grows with PM
- Many MM >> PM
- log scale stabilises variance

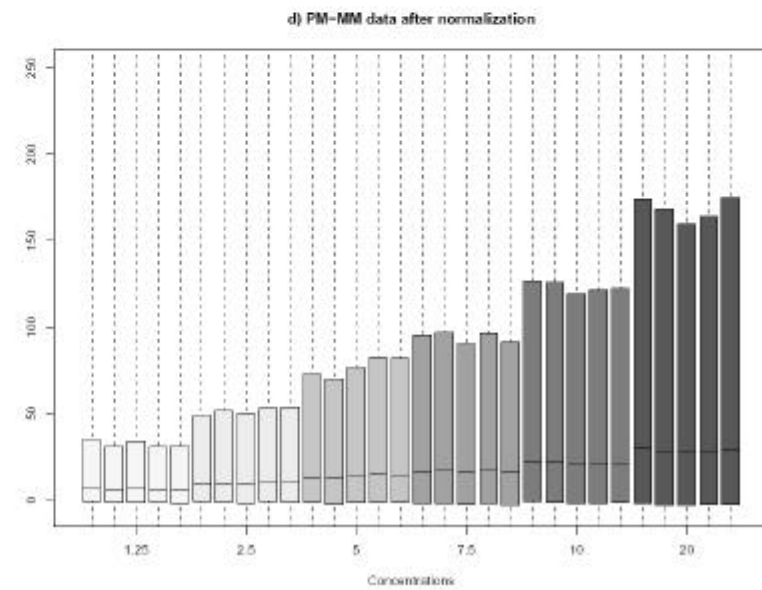
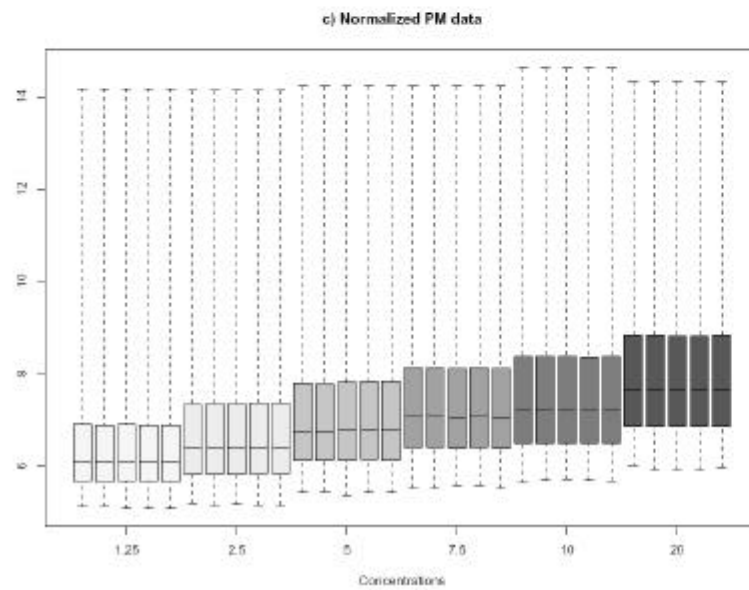
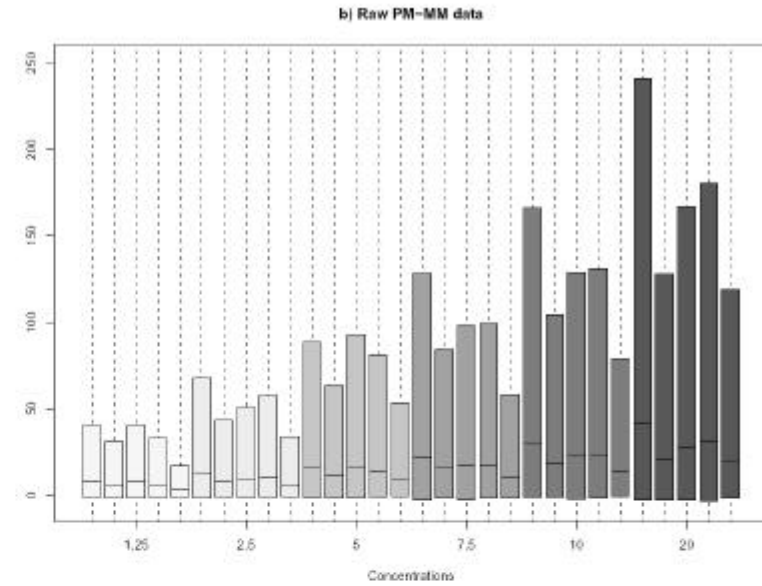
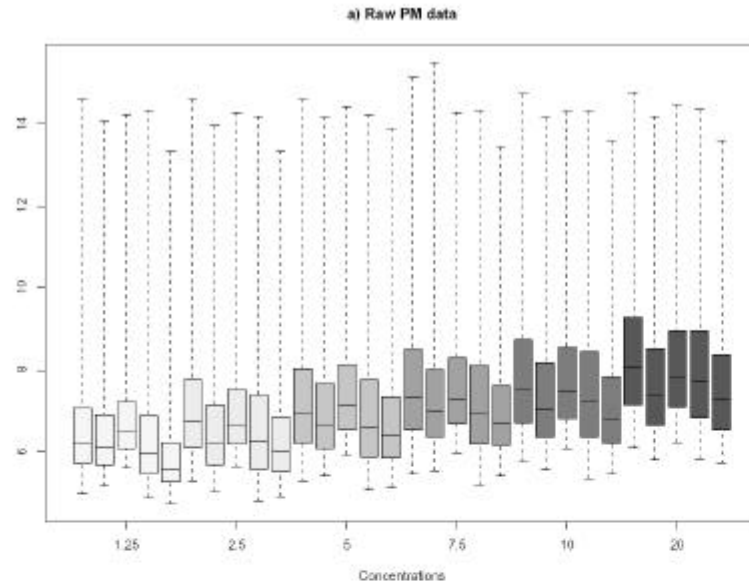
$$M = \log_2(\text{PM}/\text{MM})$$

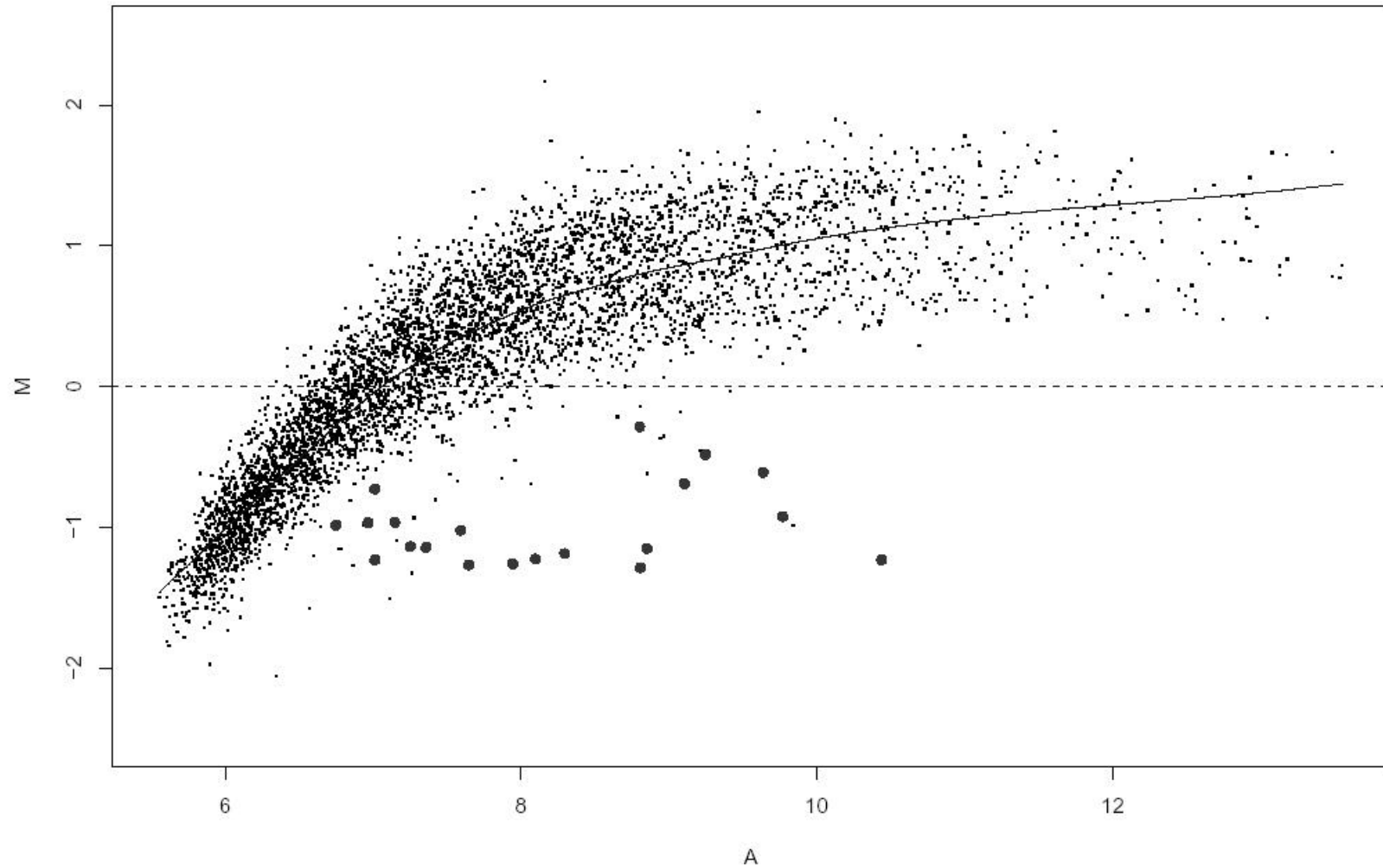
$$A = 0.5 \cdot \log_2(\text{PM} \cdot \text{MM})$$

abundance



# Dilution data





$$M = \log_2(\text{PM}_1 / \text{PM}_2) \quad A = 0.5 \cdot \log_2(\text{PM}_1 \cdot \text{PM}_2)$$

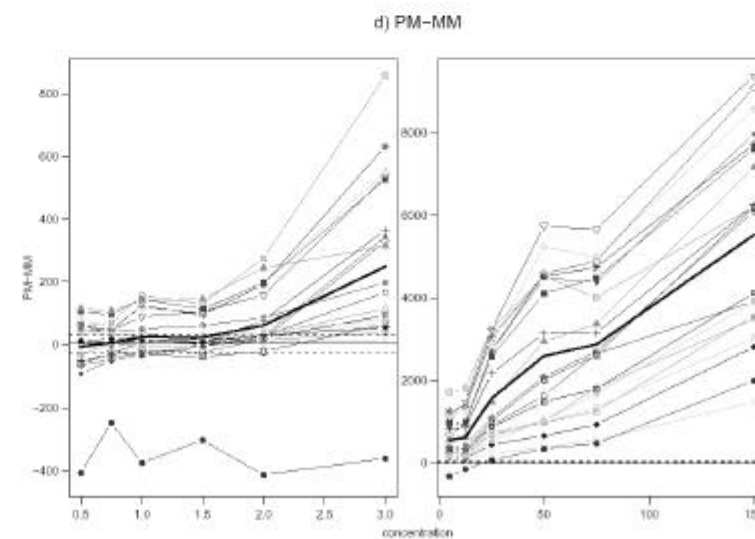
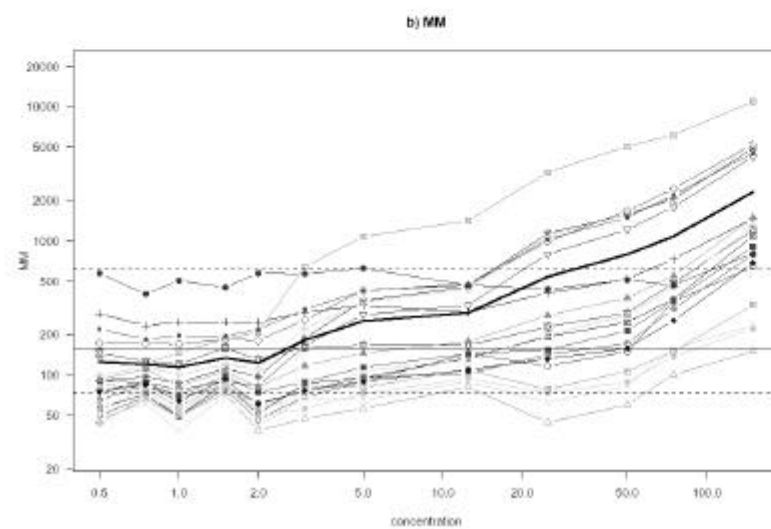
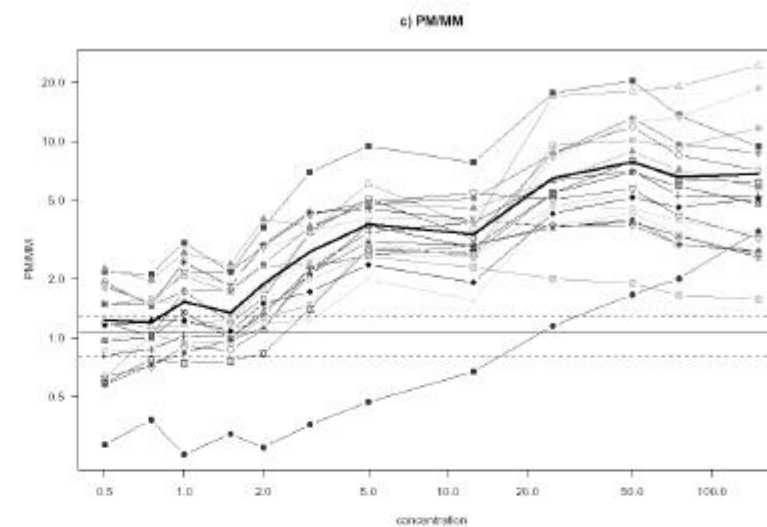
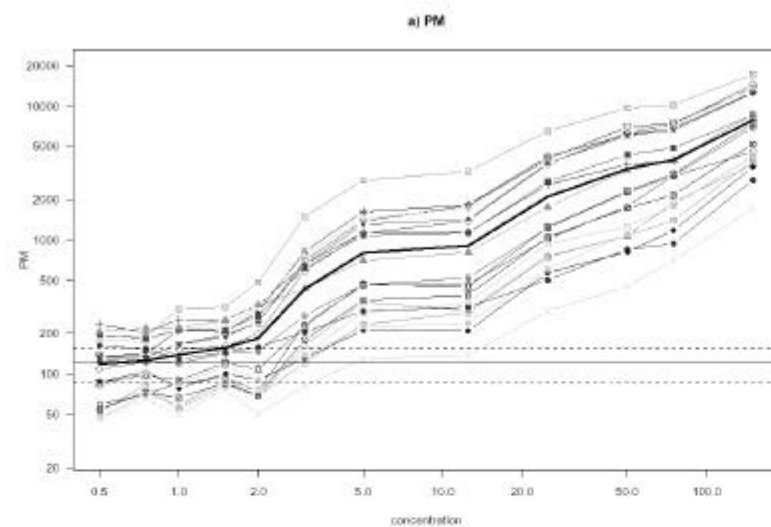
Bland-Altman plots

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## Arguments against the use of $d = PM-MM$

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- Difference is more variable. Is there a gain in bias to compensate for the loss of precision?
- MM detects signal as well as PM
- PM / MM results in a bias.
- Subtraction of MM is not strong enough to remove probe effects, nothing is gained by subtraction

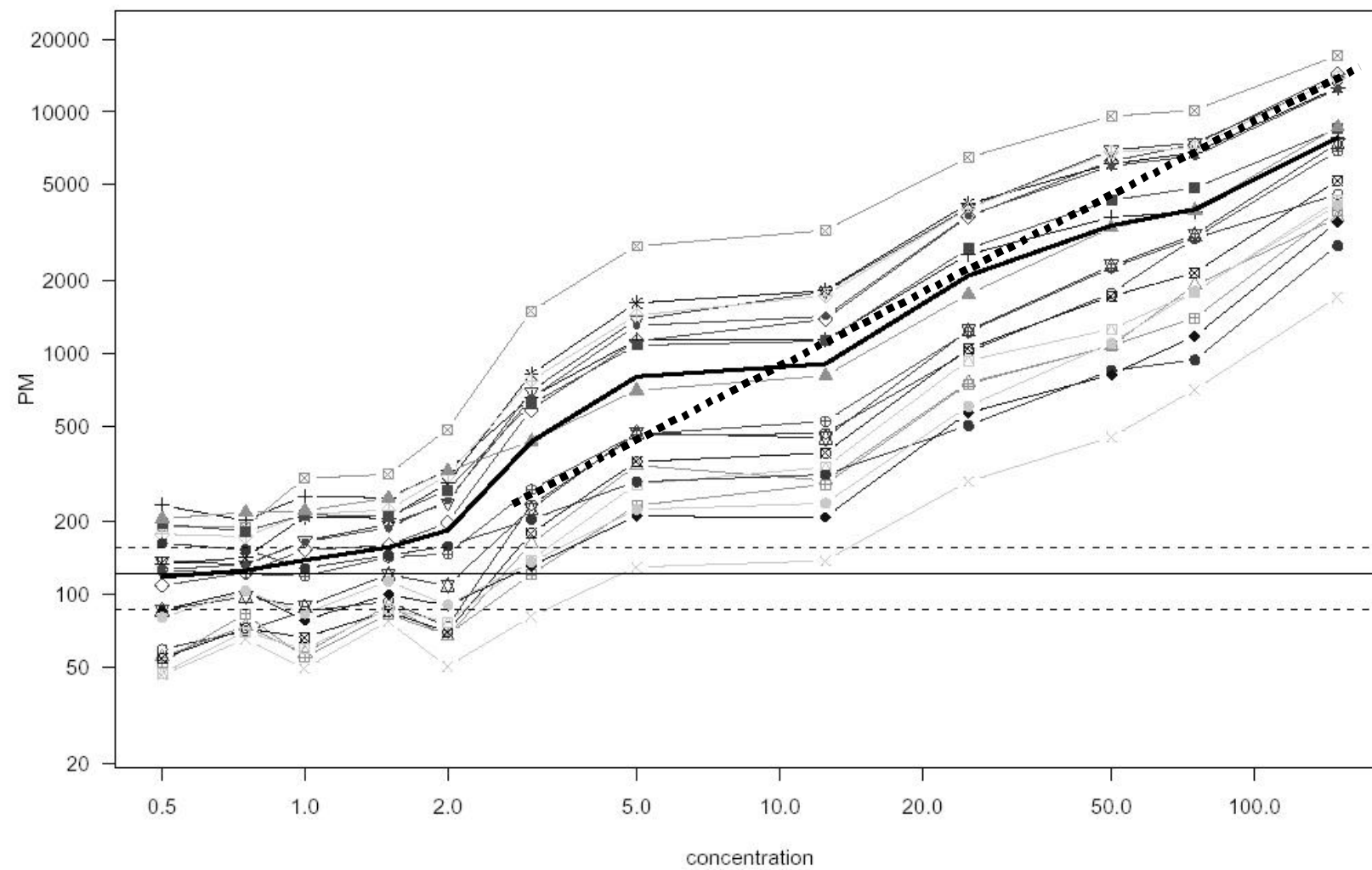


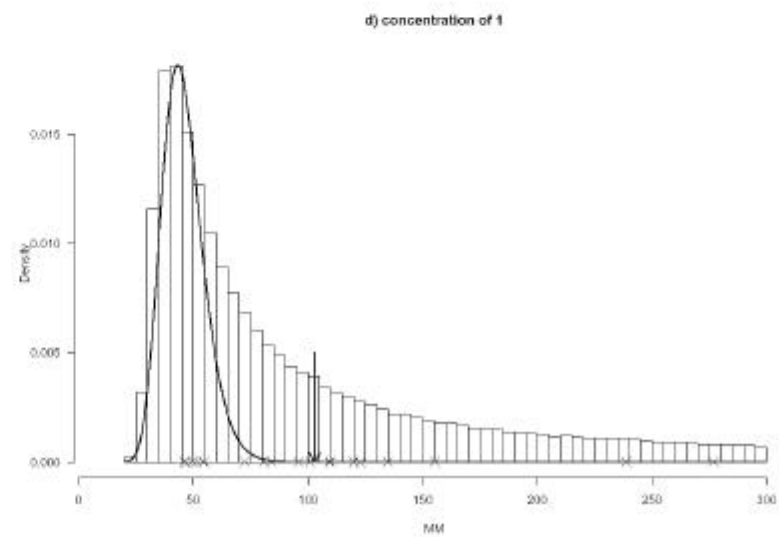
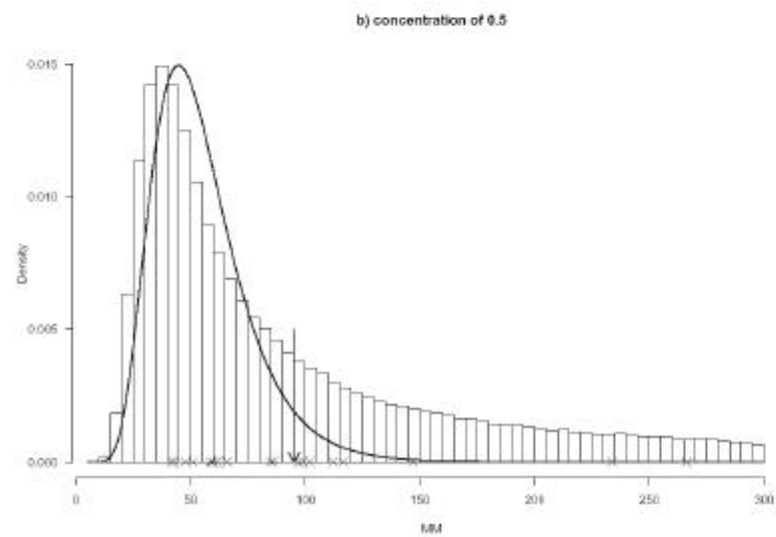
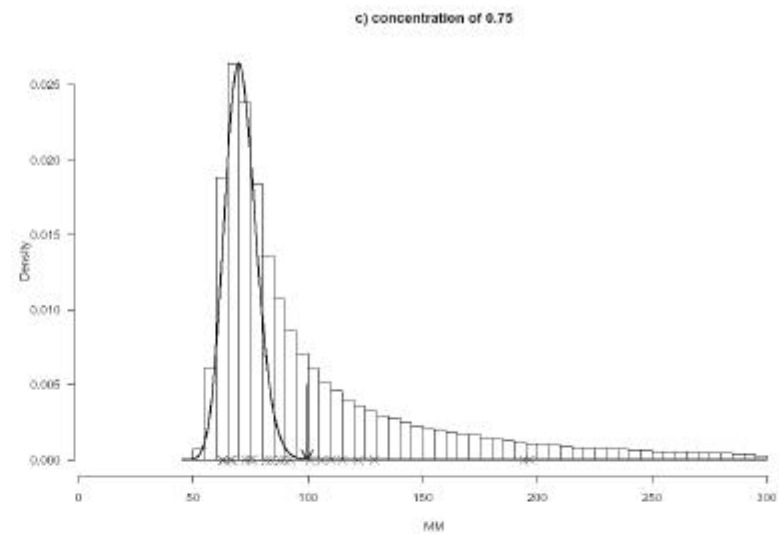
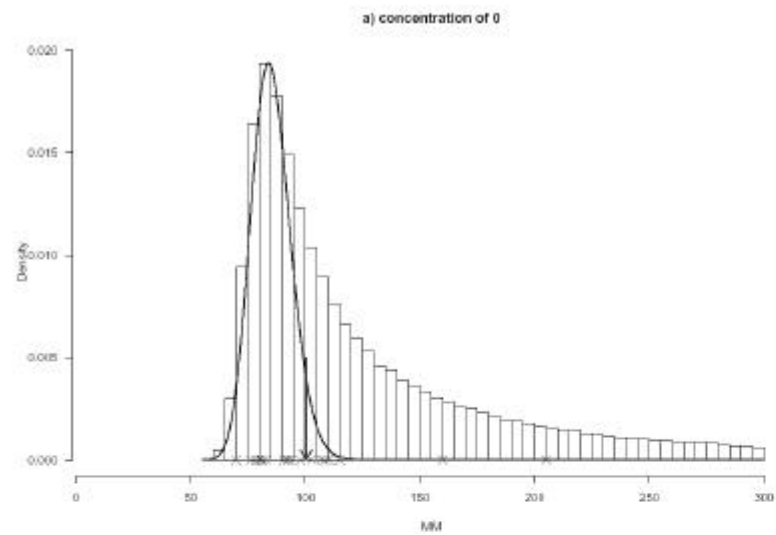
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## Expression measure based on PM only

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- Use PM values but correct for unspecific binding and background (optical) noise.  
For small signals uncorrected values may give misleading results:  
 $\log_2(100+2s) - \log_2(100+s)$  versus  $\log_2(2s) - \log_2(s)$
- $PM_{ijn} = bg_{ijn} + s_{ijn}$
- Basic idea:  
Correct by  $PM_{ijn} - b_i$  with  $\log_2(b_i)$  equal to the mode of  $\log_2(MM)$
- Advanced idea:  
 $B(PM_{ijn}) = E[s_{ijn} | PM_{ijn}]$  with  $s_{ijn}$  exponential and  $bg_{ijn}$  normally distributed. This problem has an explicit solution and gives a closed form transformation B.





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## The RMA procedure

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- Robust multi-array average
- Background corrections for array using transformation B
- Normalise the arrays by using quantile normalisation
- Use the background adjusted, normalised, log-transformed PM intensities (Y) and follow a linear model:

$$Y_{ijn} = \mu_{in} + \alpha_{jn} + \varepsilon_{ijn}$$

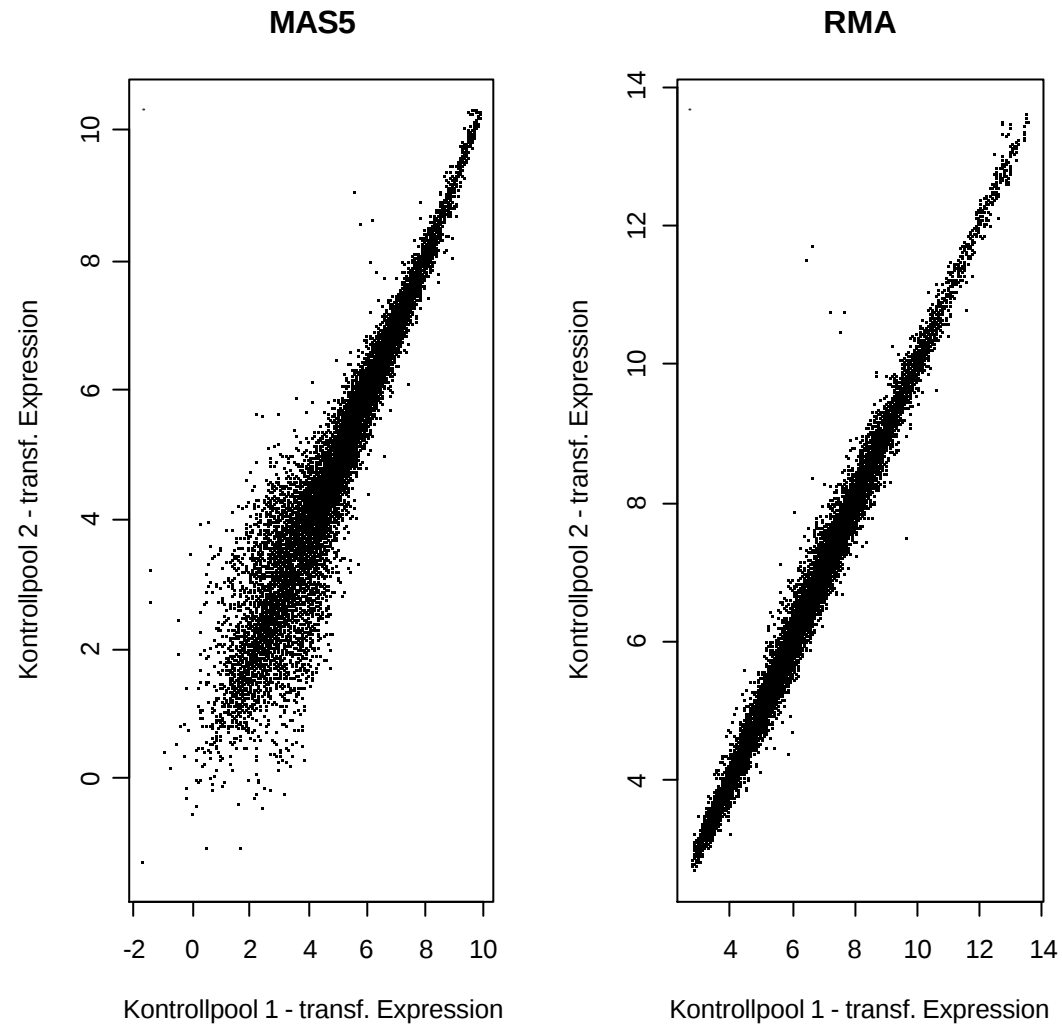
where  $\alpha_{jn}$  is the probe affinity,  $\sum \alpha_{jn} = 0$  for all n  
 $\mu_{in}$  is the log scale expression level  
 $\varepsilon_{ijn}$  is an error with mean 0

Irizarry et al. (2002) [www.biostat.jhsph.edu/~rirzarr/affy](http://www.biostat.jhsph.edu/~rirzarr/affy)

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## Example LPS: *Expression Summaries*

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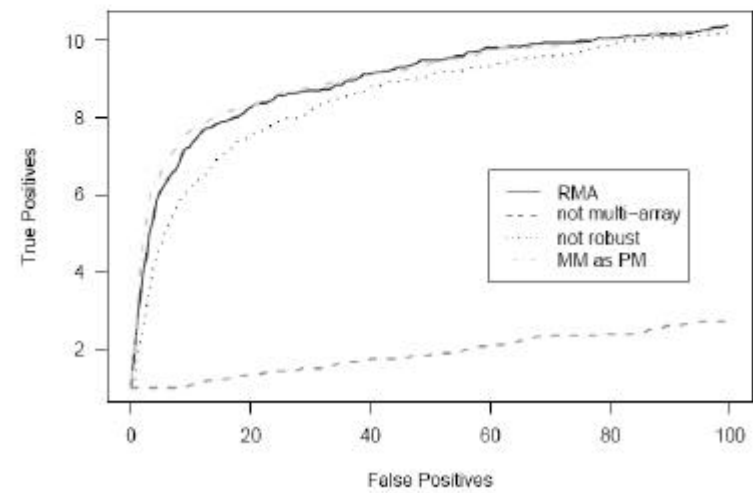
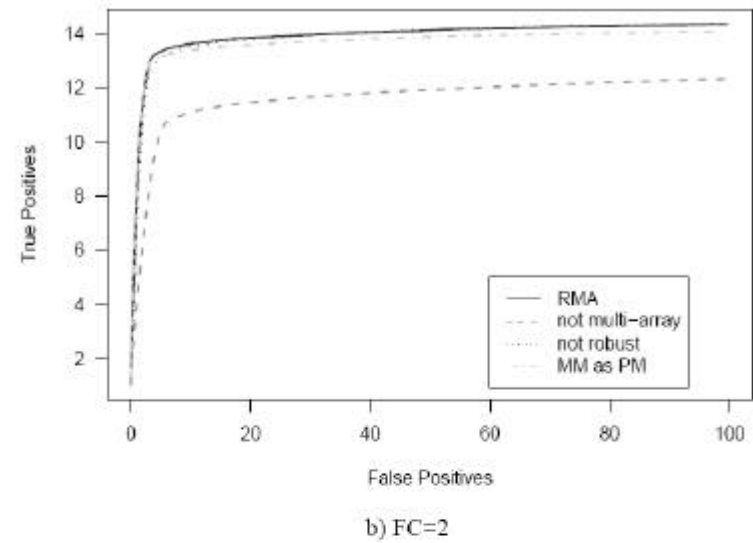
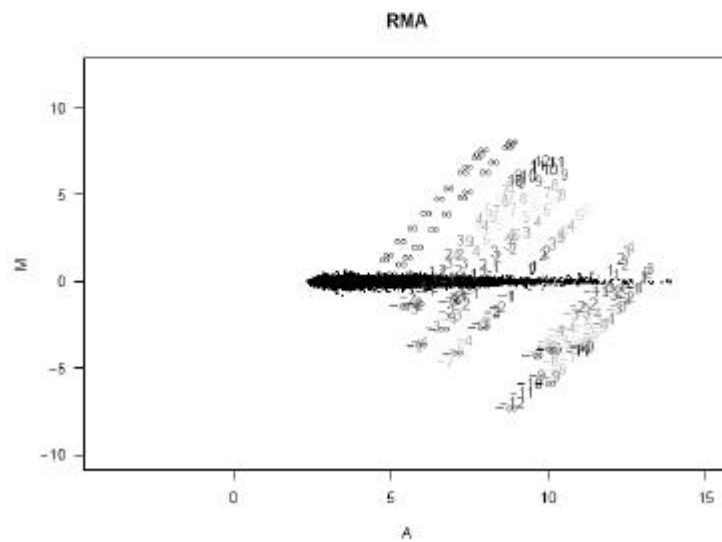
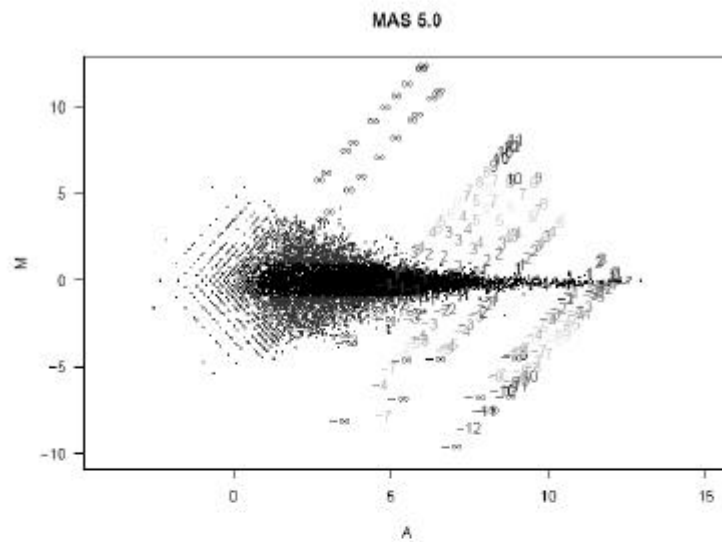
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## AffyComp

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- Graphical tool to evaluate summaries of Affymetrix probe level data.
- Plots and summary statistics
- Comparison of competing expression measures
- Selection of methods suitable for a specific investigation
- Use of benchmark data sets

What makes a good expression measure: leads to good and precise answers to a research question.



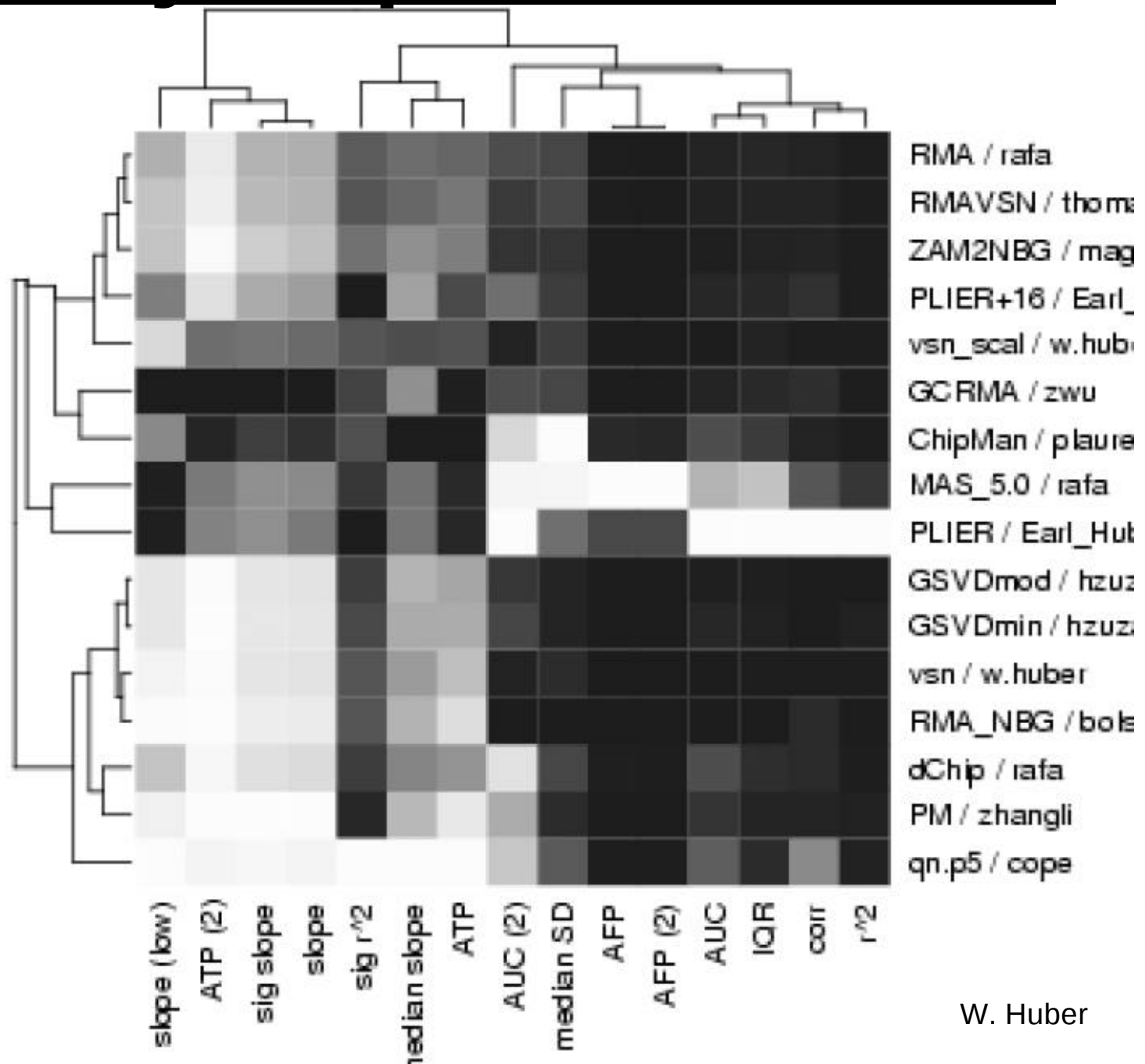
```
> affycompTable(rma.assessment, mas5.assessment)
```

|                         | RMA         | MAS.5.0      | whatsgood | Figure |
|-------------------------|-------------|--------------|-----------|--------|
| Median SD               | 0.08811999  | 2.920239e-01 | 0         | 2      |
| R2                      | 0.99420626  | 8.890008e-01 | 1         | 2      |
| 1.25v20 corr            | 0.93645083  | 7.297434e-01 | 1         | 3      |
| 2-fold discrepancy      | 21.00000000 | 1.226000e+03 | 0         | 3      |
| 3-fold discrepancy      | 0.00000000  | 3.320000e+02 | 0         | 3      |
| Signal detect slope     | 0.62537111  | 7.058227e-01 | 1         | 4a     |
| Signal detect R2        | 0.80414899  | 8.565416e-01 | 1         | 4a     |
| Median slope            | 0.86631340  | 8.474941e-01 | 1         | 4b     |
| AUC (FP<100)            | 0.82066051  | 3.557341e-01 | 1         | 5a     |
| AFP, call if fc>2       | 15.84156379 | 3.108992e+03 | 0         | 5a     |
| ATP, call if fc>2       | 11.97942387 | 1.281893e+01 | 16        | 5a     |
| FC=2, AUC (FP<100)      | 0.54261364  | 6.508575e-02 | 1         | 5b     |
| FC=2, AFP, call if fc>2 | 1.00000000  | 3.072179e+03 | 0         | 5b     |
| FC=2, ATP, call if fc>2 | 1.71428571  | 3.714286e+00 | 16        | 5b     |
| IQR                     | 0.30801579  | 2.655135e+00 | 0         | 6      |
| Obs-intended-fc slope   | 0.61209902  | 6.932507e-01 | 1         | 6a     |
| Obs-(low)int-fc slope   | 0.35950904  | 6.471881e-01 | 1         | 6b     |

# u affycomp results (28 Sep 2003)

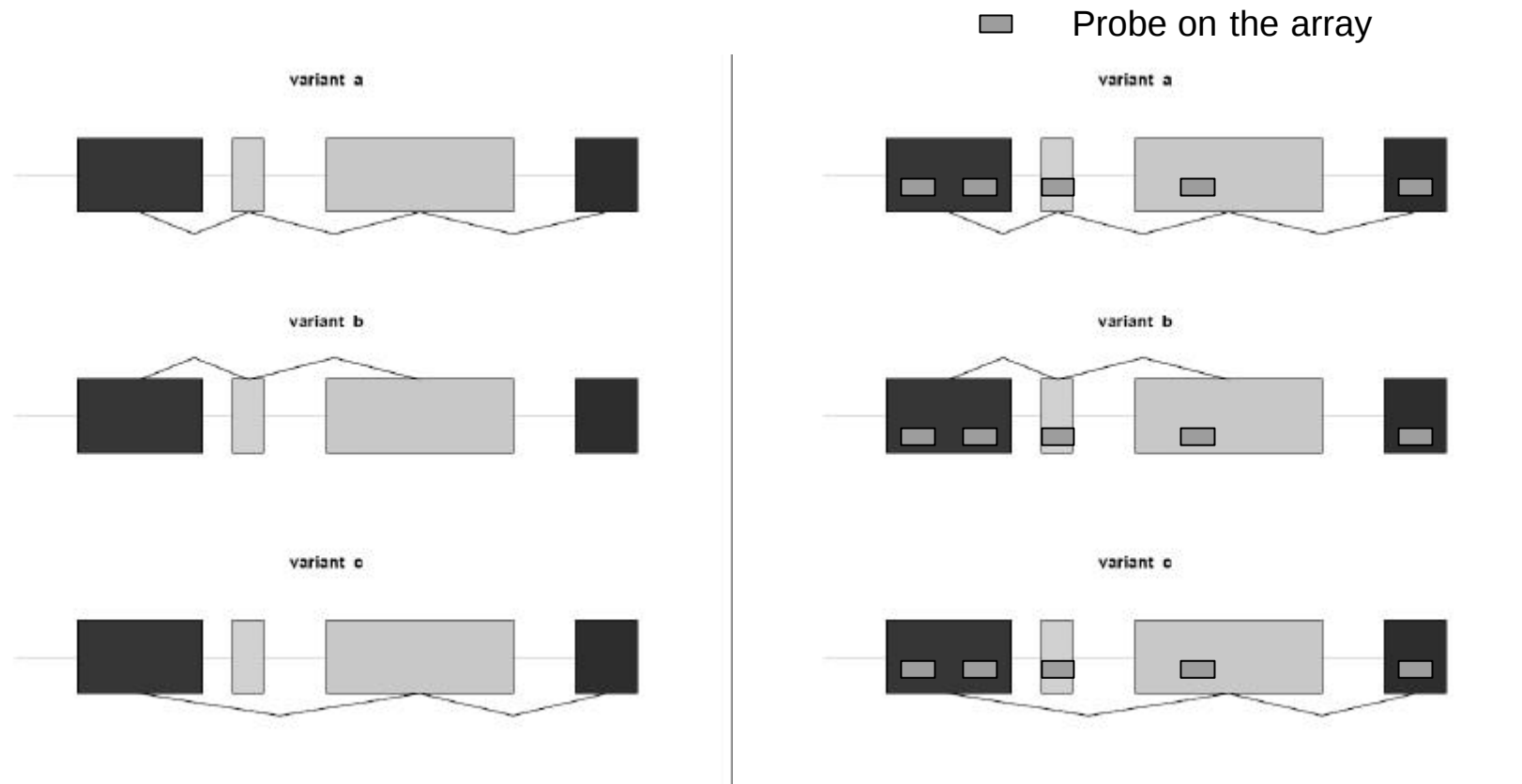
good

bad



W. Huber

# Alternative Splicing



A popular representation of splice variants shows exons as boxes, linked by broken lines to show which exons are skipped and which ones are not for the splice variants.

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# Alternative Splicing

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hgu95av2probe {hgu95av2probe}

R Documentation

## Probe sequence for microarrays of type hgu95av2.

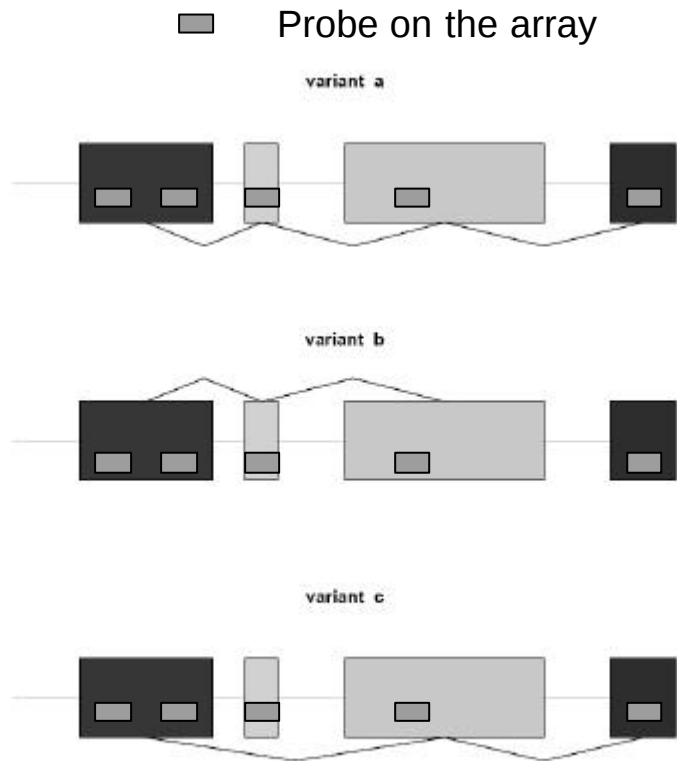
**Description:** This data object was automatically created by the package matchprobes version 0.8.3.

**Usage:** data(hgu95av2probe)

**Format:** A data frame with 199084 rows and 6 columns, as follows.

|                              |                                       |
|------------------------------|---------------------------------------|
| sequence                     | character probe sequence              |
| x                            | integer, x-coordinate on the array    |
| y                            | integer, y-coordinate on the array    |
| Probe.Set.Name               | character, Affymetrix Probe Set Name  |
| Probe.Interrogation.Position | integer, Probe Interrogation Position |
| Target.Strandedness          | factor, Target Strandedness           |

# Alternative Splicing



## Expression measurement

| $P_1$ | $P_2$ | $P_3$ | $P_4$ | $P_5$ |       |
|-------|-------|-------|-------|-------|-------|
| H     | H     | H     | H     | H     | $V_a$ |
| H     | H     | H     | H     | L     | $V_b$ |
| H     | L     | H     | H     | H     | $V_c$ |

Techniques from Discriminant Analysis help to calculate discriminatory scores to identify a certain variant with an array.

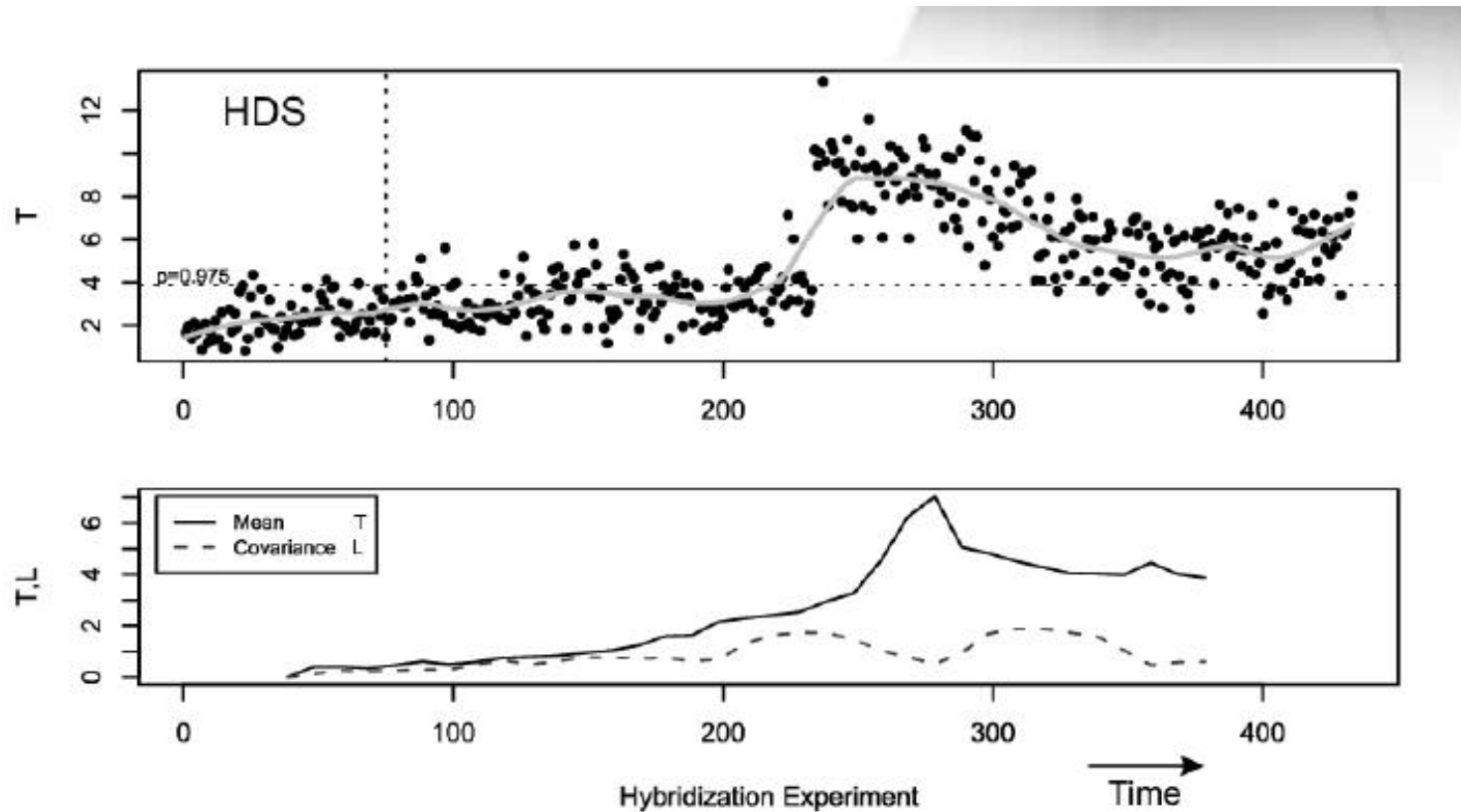
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## Process Control for large scale experiments

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- Model F. et al. (2002) Bioinformatics, 18:S155-163
- HDS: historical data set, variables of a process for some time under perfect working conditions. CDS: current data set.
- How far is the current state of the process away from the perfect state?
- Distance measure: Hotelling's  $T^2 = (m - \mu)^t S^{-1} (m - \mu)^t$   
parameter  $\mu$  and  $S$  estimated from the HDS
- Additional tasks:
  1. outlier treatment with robust Principle Component Analysis (rPCA)  
The estimates  $\mu$  and  $S$  are not robust against outliers
  2. For fewer arrays than number of gene expression, the sample covariance matrix  $S$  is singular and not invertible.  
PCA is used to reduce dimensionality of the measurement space.
- Calculate an upper control limit to initiate interventions in the ongoing process.
- In order to see whether an observed change in  $T^2$  comes from a simple translation, it is of interest to compare the two sample covariances between HDS and CDS.  
A LRT for different covariances is used, calculates statistic  $L$  ( $H_0: L=0$ )

# Process Control for large scale experiments



$T^2$  control chart of ALL/AML study. Over the course of the experiment a total of 46 oligomers for 35 different CpG positions had to be re-synthesized.

*They all talked at once, their voices insistent and contradictory and impatient, making of unreality a possibility, then a probability, than an incontrovertible fact, as people will when their desires become words.*

Willian Faulkner, *The sound and the fury*, 1929