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# Kinetic modelling helps to understand oxidative stress caused by an antioxidant

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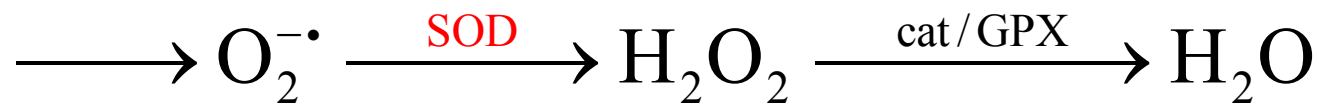
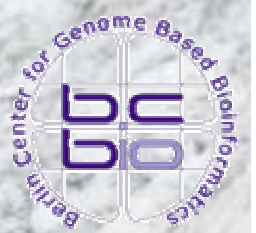
# Trisomy21 (Down Syndrome)



- Three copies of chromosome 21
- First described 1866 by J. L. Down
- Genetic basis discovered 1959
- Prevalence ca. 1:800
- Mental retardation and characteristic facial features
- Overexpression of the ca. 250 genes of chromosome 21
- Genes with possible relevance for Down Syndrome: **SOD**, COL6A1, ETS2, CAF1A, CBS, DYRK, CRYA1, GART, IFNAR



# Superoxide Dismutase



$$\frac{d\text{O}_2^{\bullet -}}{dt} = k_1 - k_2 \cdot \text{SOD} \cdot \text{O}_2^{\bullet -}$$

$$\frac{d\text{H}_2\text{O}_2}{dt} = k_2 \cdot \text{SOD} \cdot \text{O}_2^{\bullet -} - k_3 \cdot \text{cat} \cdot \text{H}_2\text{O}_2$$



$$\text{O}_{2,ss}^{\bullet -} = \frac{k_1}{k_2 \cdot \text{SOD}}$$

$$\text{H}_2\text{O}_{2,ss} = \frac{k_1}{k_3 \cdot \text{cat}}$$



# Negative Effects



- Increased lipid peroxidation in Trisomy21
- Increased lipid peroxidation in cell cultures
- Increased mortality in transgenic *D. melanogaster*
- Lipid peroxidation, diminished prostaglandin synthesis and serotonin uptake in transgenic mice.
- Bacteria overexpressing SOD showed increased paraquat sensitivity.



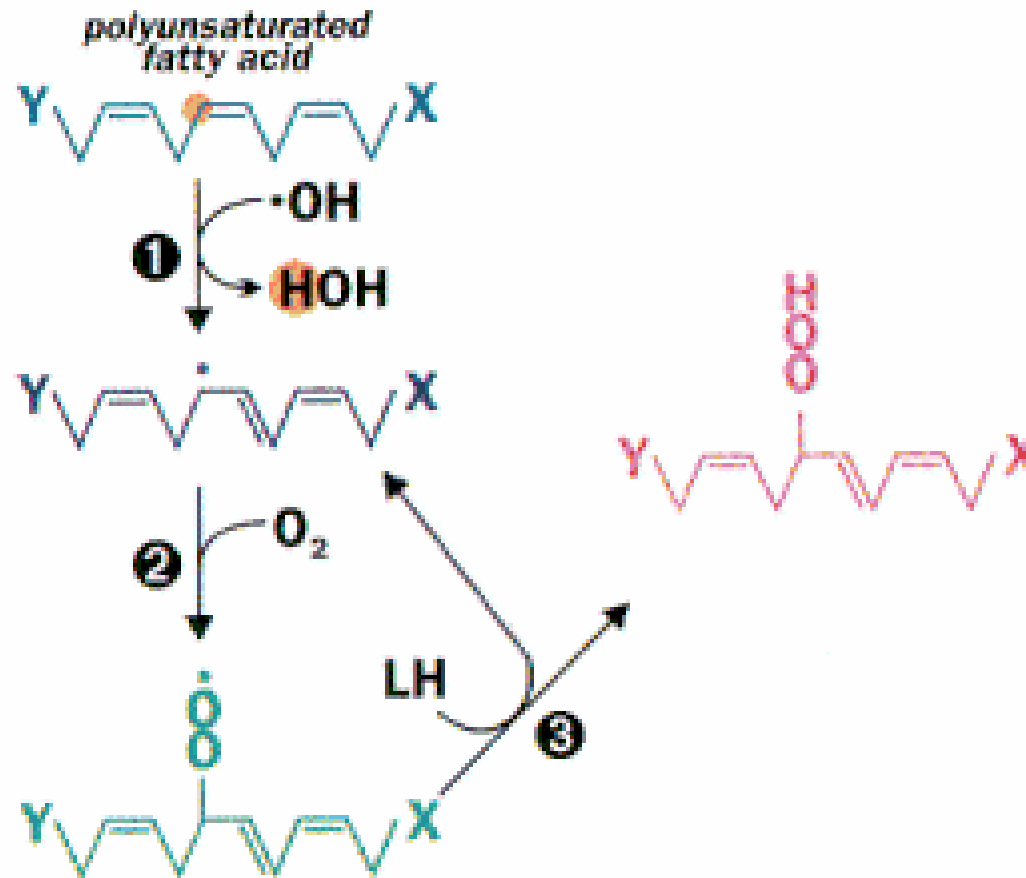
# Explanations



- The reaction of  $\text{H}_2\text{O}_2$  with CuZnSOD leads to hydroxyl radical generation.
- $\text{O}_2^{*-}$  radicals might reduce membrane damage by acting as chain breakers.



# Lipid Peroxidation Chain Reaction





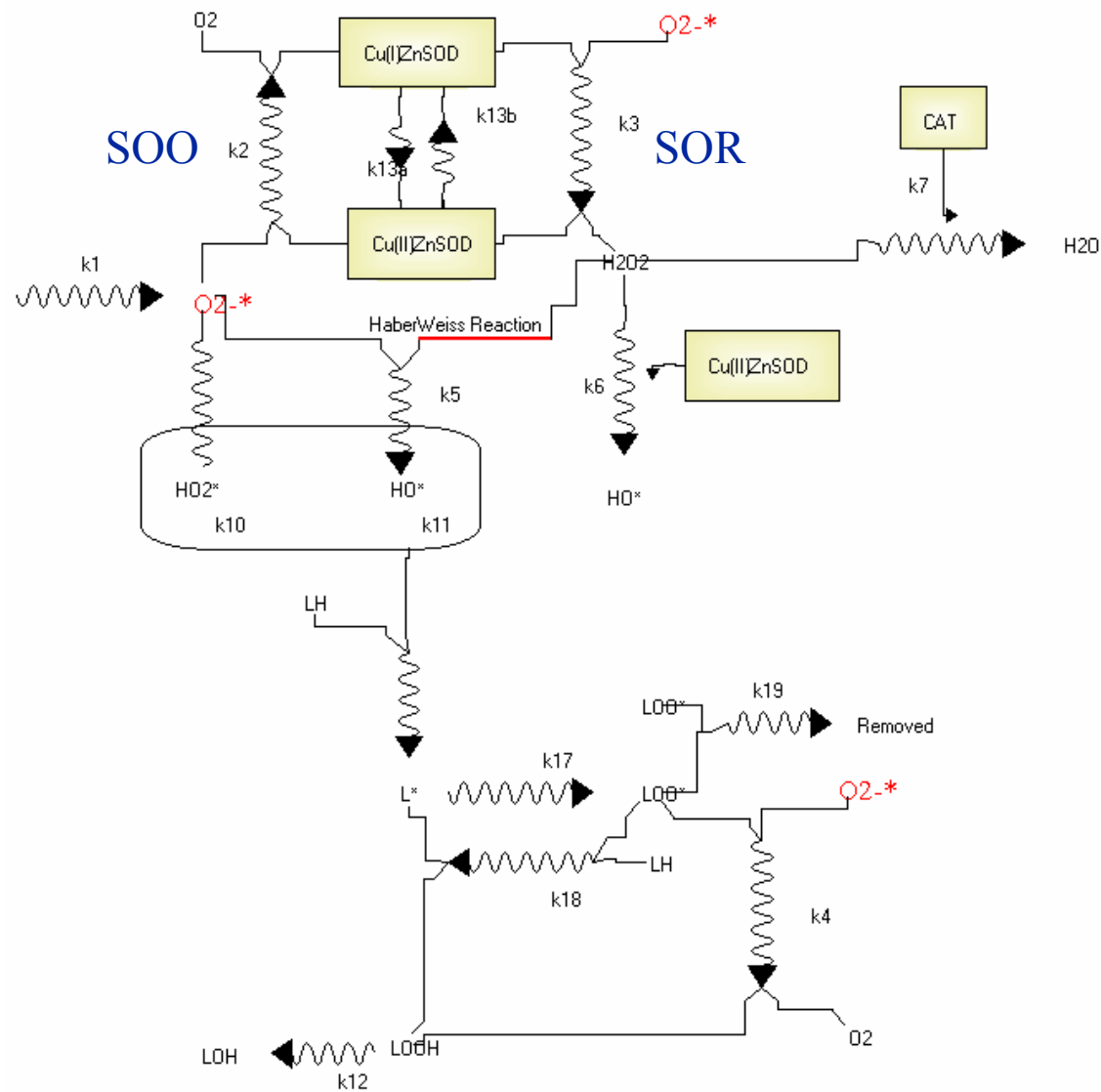
# Explanations



- The reaction of  $\text{H}_2\text{O}_2$  with CuZnSOD leads to hydroxyl radical generation.
- $\text{O}_2^{*-}$  radicals might reduce membrane damage by acting as chain breakers.
- SOD cycles between a reduced and oxidised state. At low  $\text{O}_2^{*-}$  levels the intermediates might interact with other redox partners and increase the superoxide reductase activity of SOD.

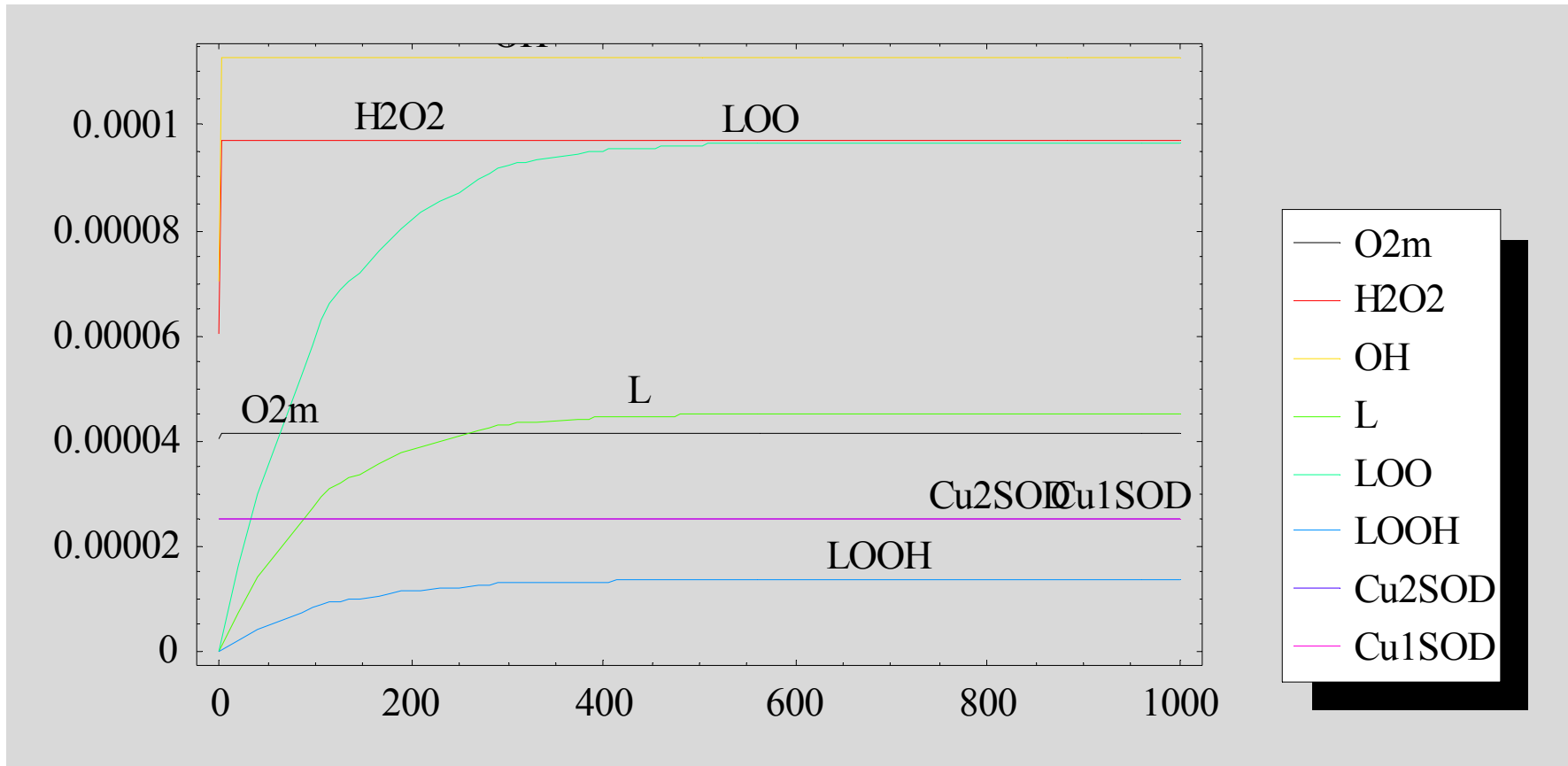


# Reactions





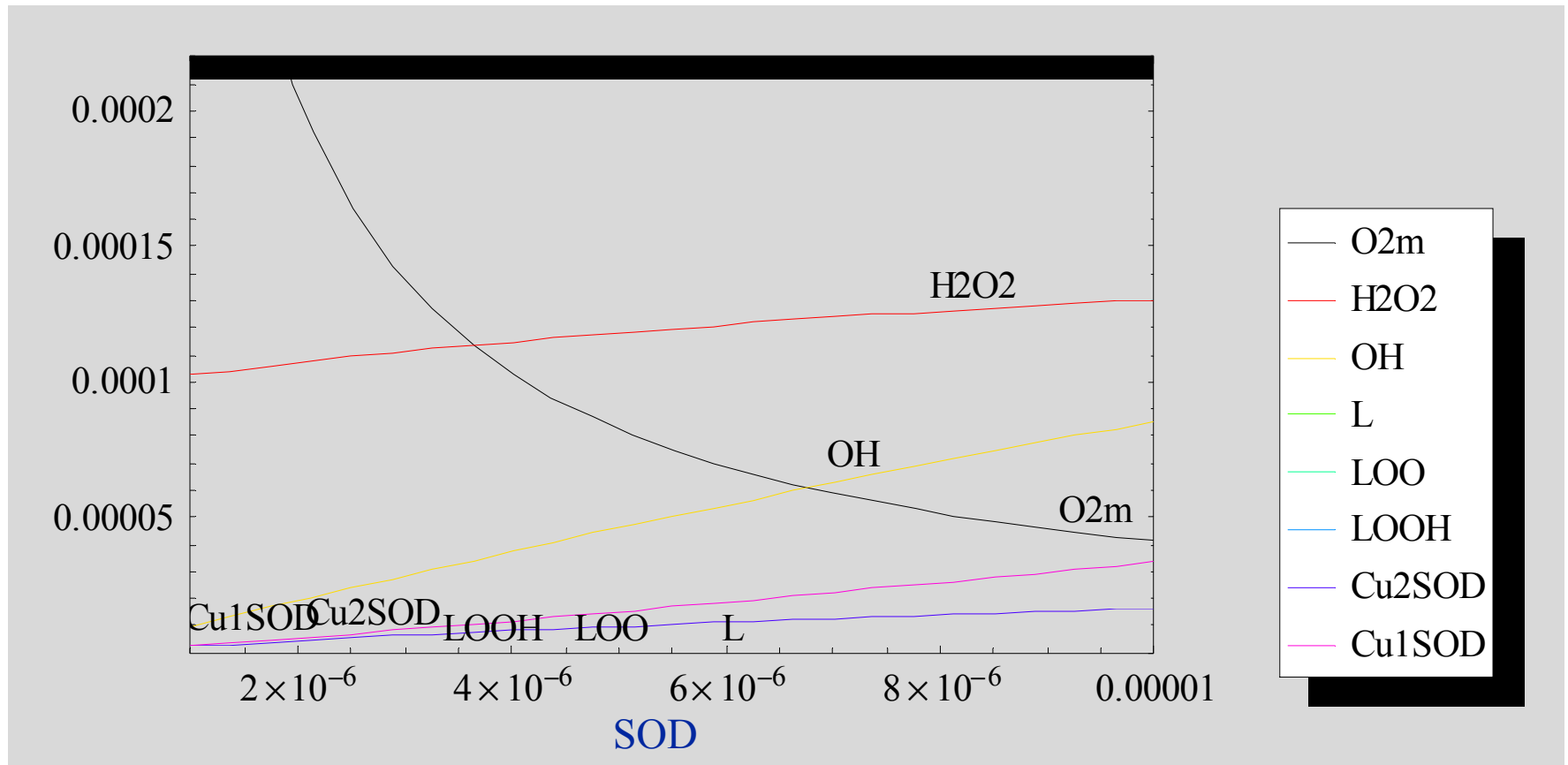
# Standard Simulation



{ $k_1 \rightarrow 6.6 * 10^{-7}$ ,  $k_2 \rightarrow 1.6 * 10^9$ ,  $k_3 \rightarrow 1.6 * 10^9$ ,  $k_4 \rightarrow 10^5$ ,  $k_5 \rightarrow 2 * 10^4$ ,  
 $k_6 \rightarrow 1$ ,  $k_7 \rightarrow 3.4 * 10^7$ ,  $k_9 \rightarrow 10^6$ ,  $k_{10} \rightarrow 2000$ ,  $k_{11} \rightarrow 5 * 10^8$ ,  $k_{12} \rightarrow 10^7 * 10^{-5}$ ,  
 $k_{13a} \rightarrow 8700 * 10^{-6}$ ,  $k_{13b} \rightarrow 8700 * 10^{-6}$ ,  $k_{17} \rightarrow 3 * 10^8$ ,  $k_{18} \rightarrow 14$ ,  $k_{19} \rightarrow 8.8 * 10^4$ ,  
 $SOD \rightarrow 10^{-5}$ ,  $cat \rightarrow 10^{-5}$ }



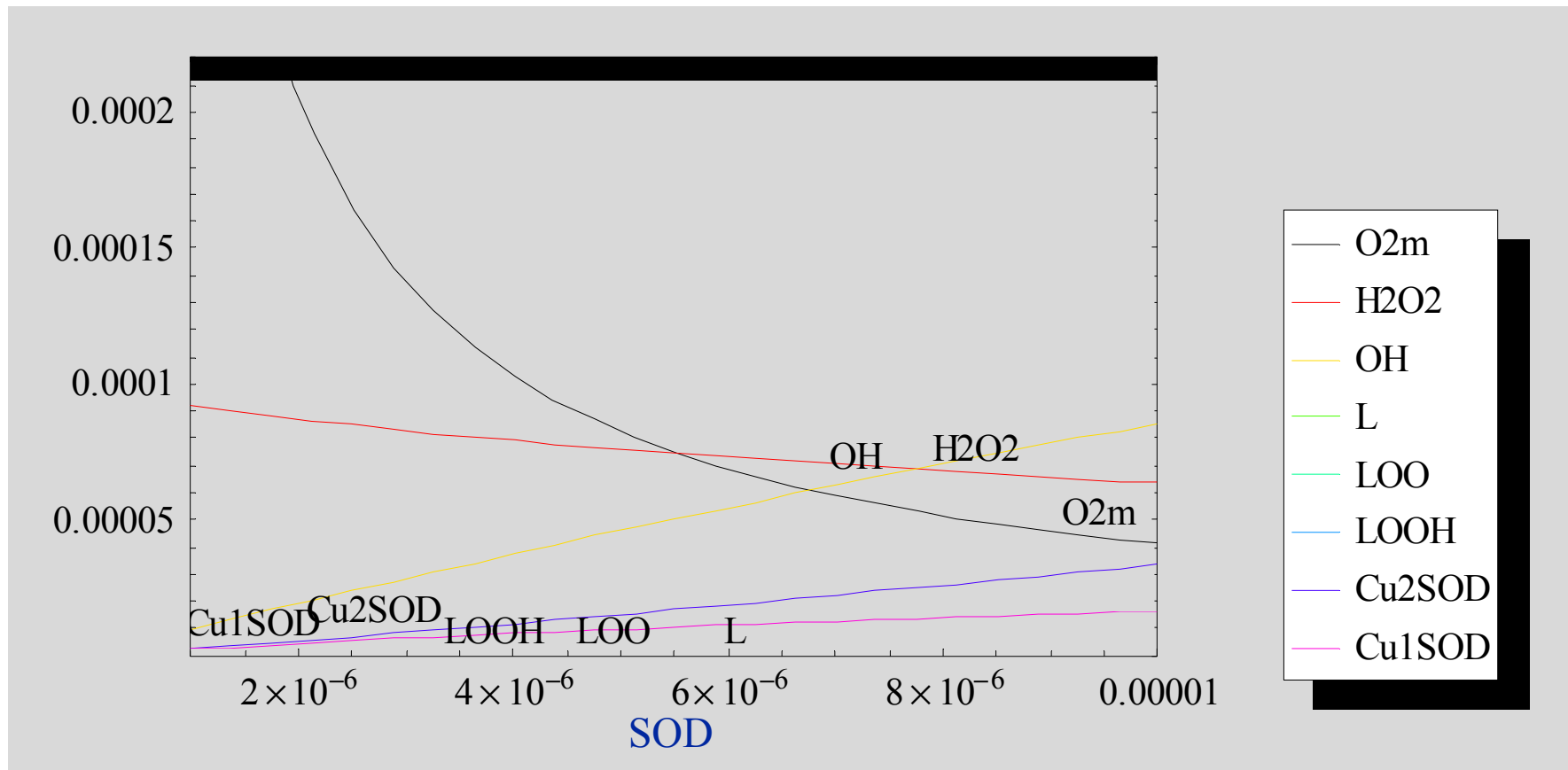
# Increasing SOR Activity



$$k3b = 10 * k3a$$



# Increasing SOD Activity



$$10 \cdot k_{3b} = k_{3a}$$



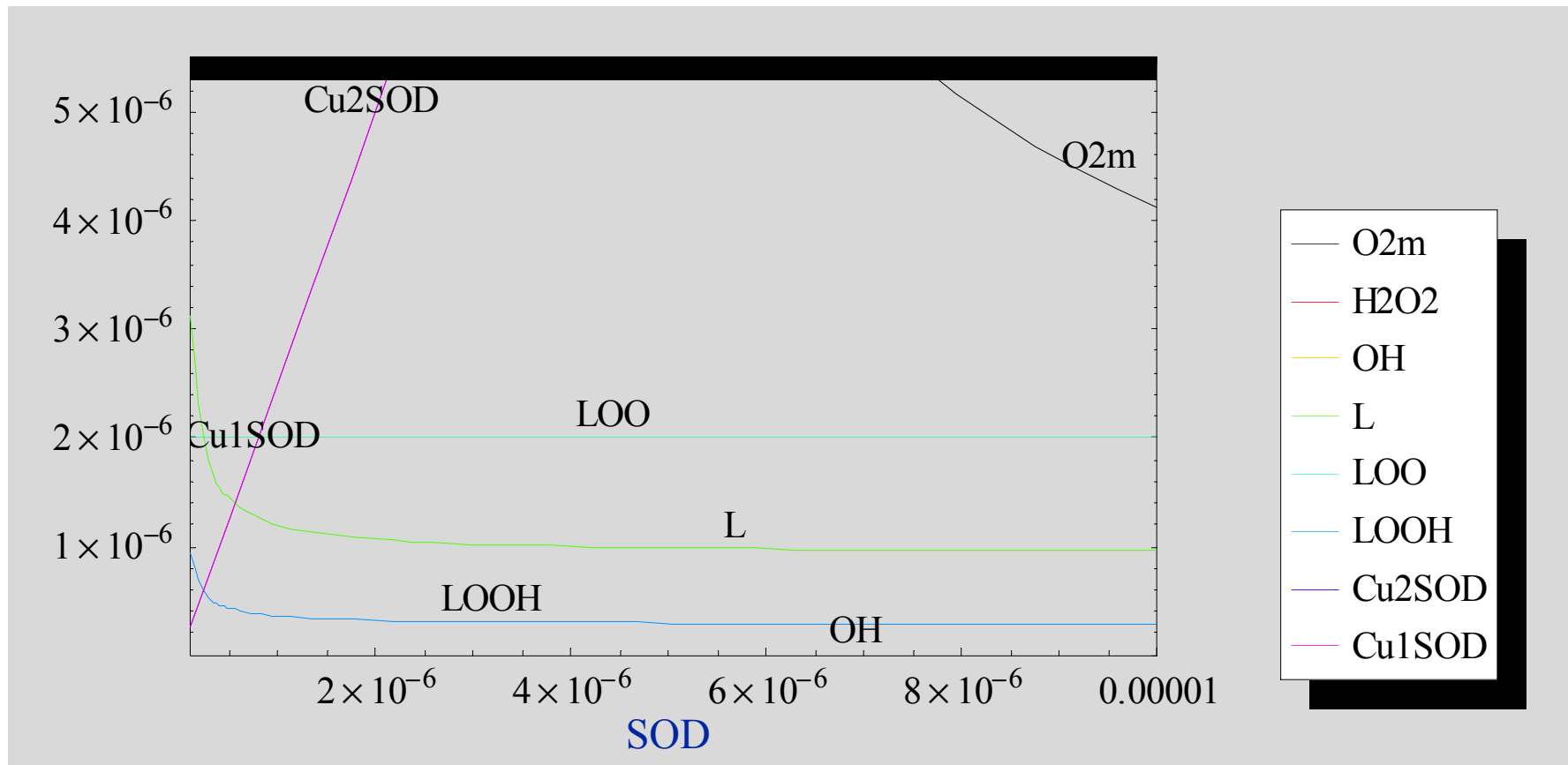
# SOO/SOR Results



- In principle the SOO/SOR idea works.
- However, it is not clear why in experiments SOR activity is always greater than SOO activity.
- Alternative redox partners have only been demonstrated for CuZnSOD, not MnSOD.



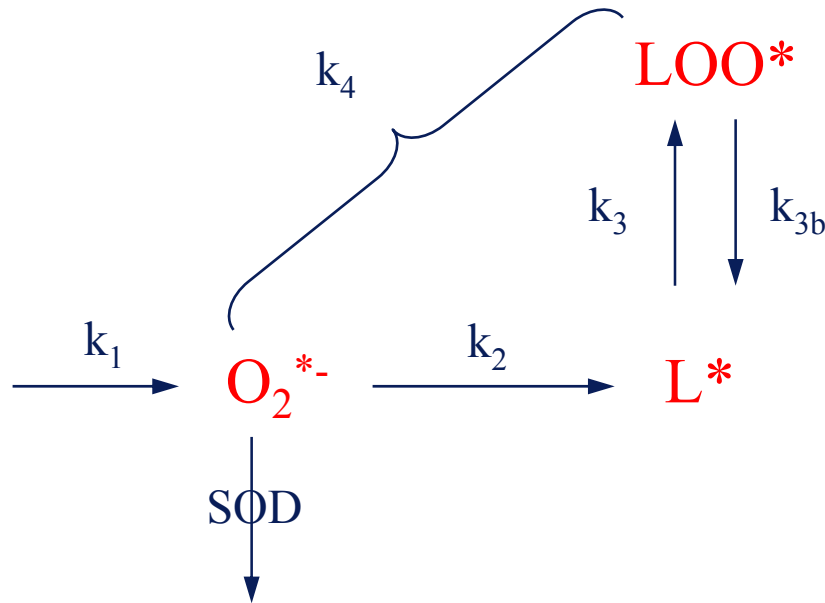
# Membrane Damage Termination



- LOO\* remains constant throughout the entire range
- L\* and LOOH increase for small SOD values, but are constant otherwise.
- Why are the concentrations of L\* and LOO\* not increasing with increasing SOD ? 13



# Simplified Modell



$$O_{2,ss}^{\bullet-} = \frac{k_1}{2k_2 + SOD}$$

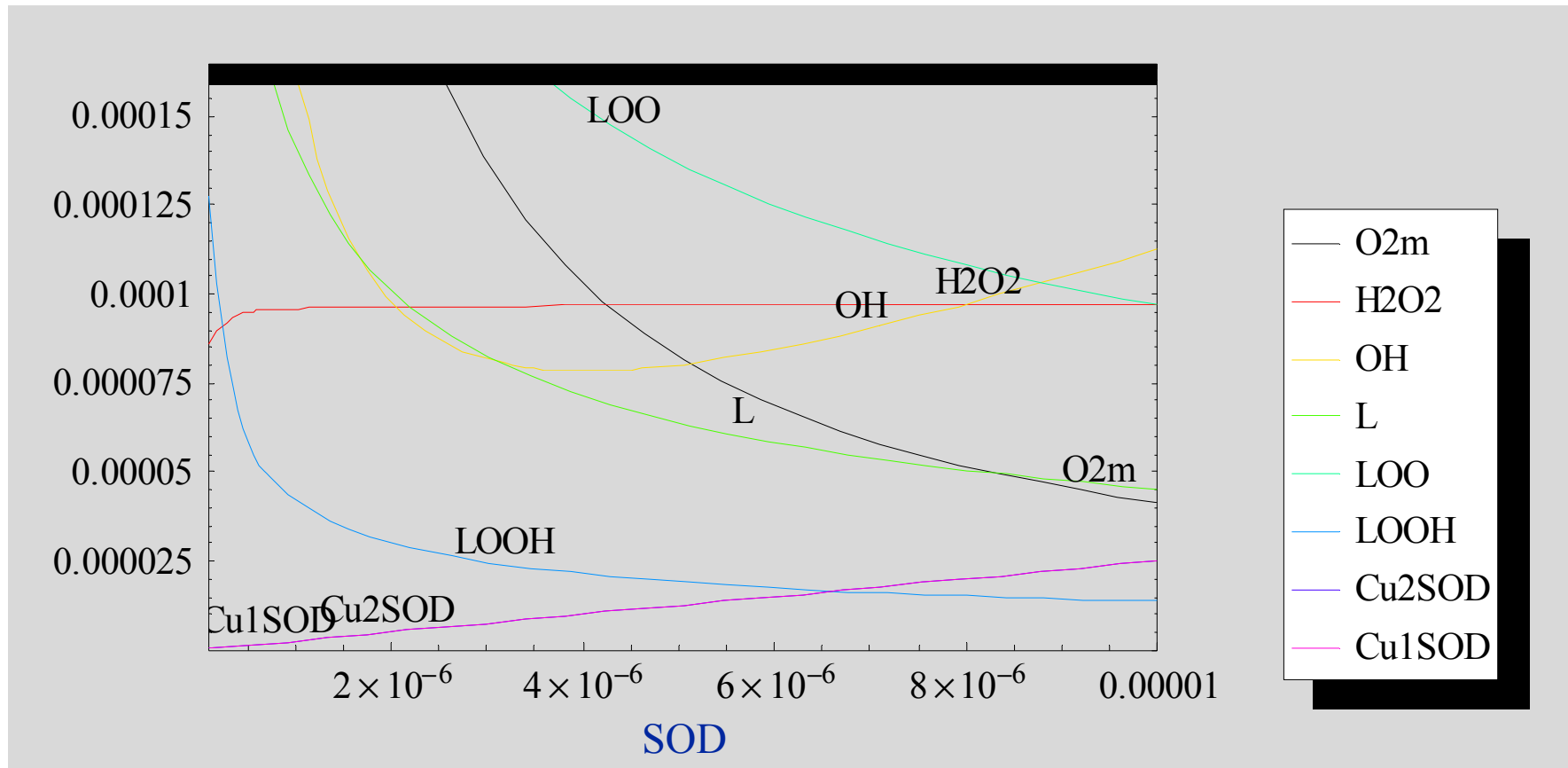
$$LOO_{ss}^{\bullet} = \frac{k_2}{k_4}$$

$$L_{ss}^{\bullet} = \frac{k_2 \cdot k_{3b}}{k_3 \cdot k_4} + \frac{k_1 \cdot k_2}{k_3 \cdot (2k_2 + SOD)}$$

- $LOO^*$  doesn't change because it is completely independent of  $SOD$  and  $O_2^{*-}$ . If the concentration of  $O_2^{*-}$  changes, membrane damage initiation changes by the same factor as the termination (for a given  $k_4$ ).
- Without the back reaction  $k_{3b}$ , levels of  $L^*$  should decrease continuously with increasing  $SOD$ , and this can be confirmed by disabling this reaction in the full modell.
- => Chain breaker idea does not work !!



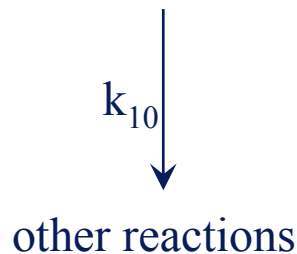
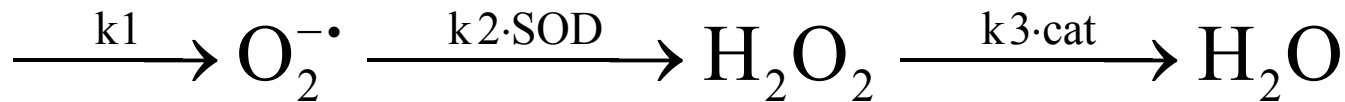
# Alternative Pathway Mechanism



Simulation with full model and SOO equal to SOR (no effect)



# Simplified Modell 2



$$\text{O}_{2,ss}^{\bullet -} = \frac{k_1}{k_{10} + k_2 \cdot \text{SOD}}$$

$$\text{H}_2\text{O}_{2,ss} = \frac{k_1 \cdot k_2 \cdot \text{SOD}}{(k_{10} + k_2 \cdot \text{SOD}) \cdot k_3 \cdot \text{cat}}$$

- If there are alternative reaction pathways for the superoxide radical, increasing SOD channels more of the available  $\text{O}_2^{\bullet -}$  into the  $\text{H}_2\text{O}_2$  generating branch and can thus increase oxidative stress.
- This principle is independent of the SOD type (CuZnSOD, MnSOD).
- $k_{10}$  does not only represent membrane damage, but ALL other reactions of  $\text{O}_2^{\bullet -}$ . Therefore  $k_{10}$  can be much larger than the value used in the model and so the resulting effect on  $\text{H}_2\text{O}_2$  can also be much larger.



# Summary



- Overexpression of the antioxidant SOD leads to increased oxidative stress.
- We created a mathematical model to test some possible explanations.
- Only one proposed idea (SOD cycling) works as suggested under certain conditions.
- Studying the model we discovered an additional, more general, mechanism that might account for the increased oxidative stress.